

# Interpersonal Authority in a Theory of the Firm

Eric Van den Steen\*

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## Abstract

This paper develops a theory of the firm in which a firm's centralized asset ownership and low-powered incentives give a manager 'interpersonal authority' over employees (in a world with differing priors). The paper derives such interpersonal authority as an equilibrium phenomenon. One key result is that a manager's control over critical assets – through its effect on the *level* of outside options – allows the manager to order employees what to do. The paper thus provides micro-foundations for the idea that bringing a project inside a firm gives the manager authority over that project, while – in the process – explaining concentrated asset ownership, low-powered incentives, and centralized authority as typical characteristics of firms. It also leads to a new perspective on the firm as a legal entity and, building on the insights of a parallel paper, to a new theory for firm boundaries based on the idea of break-up. A key feature of the latter theory is that firm boundaries matter even though both ex-ante investments and ex-post actions are perfectly contractible.

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## 1 Introduction

Interpersonal authority (i.e., the ability of a superior to tell her subordinates what to do) is a cornerstone of organization. It is most visibly expressed in the chain of command or in the hierarchy of authority, which is the ranking of who can tell whom what to do. As Arrow (1974) noted, 'the giving and taking of orders [...] is an essential part of the mechanism by which organizations function.' Being employed is so intertwined with a boss telling the employee what to do, that people are often said to 'become their own boss' when they strike out on their own. This raises the question how interpersonal authority and the firm relate.

The purpose of this paper is to develop a theory of the firm in which a firm's centralized asset ownership and low-powered incentives (or fixed wages) are mechanisms to give a manager interpersonal authority over employees, and to use that theory to derive implications for firm boundaries. I will say

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that one person has interpersonal authority over another person if: 1) the first person tells the second what to do, 2) this (literal) order makes the second person more likely to do what the order told him to do, and 3) the person obeying (sometimes) acts against his own beliefs or preferences. The first and second criterium distinguish interpersonal authority from other solutions to the principal-agent problem – such as pay-for-performance incentives – while the third criterion distinguishes it from simple advice. Indeed, according to Simon (1947), ‘the characteristic which distinguishes authority from other kinds of influence is [...] that a subordinate holds in abeyance his own critical faculties for choosing between alternatives and uses the formal criterion of the receipt of a command or signal as his basis for choice. . . . Obedience [...] is an abdication of choice.’<sup>1</sup> I thus use ‘authority’ in the sense of ‘the power or right to give orders and enforce obedience’ (Concise Oxford English Dictionary), which is essentially the definition given by Fayol (1916, 1949).

Note that I study here ‘interpersonal authority’ instead of the ‘decision authority’ (i.e., the ability of a manager to make a particular decision) that has been the focus of some recent literature (Marschak and Radner 1972, Milgrom and Roberts 1988, Prendergast 1995, Aghion and Tirole 1997, Baker, Gibbons, and Murphy 1999, Aghion, Dewatripont, and Rey 2004). My use of the term ‘authority’ is actually consistent with an earlier literature (Coase 1937, Simon 1947, Simon 1951).<sup>2</sup>

The idea that authority plays a central role in the nature and function of a firm has a long and respectable tradition in economics. Knight (1921), Coase (1937), Simon (1947, 1951), Arrow (1974), and Williamson (1975) all interpreted or defined the firm as being about authority. Coase (1937), for example, likens the firm to a ‘master and servant’ relationship. Alchian and Demsetz (1972), however, sharply criticized this view. In particular, they argued that ‘(the firm) has no authority (...) any different (...) from ordinary market contracting’ and that ‘(the firm) can fire or sue, just as I can fire my grocer by stopping purchases from him or sue him for delivering faulty products.’ In response to the Alchian-Demsetz critique, economists have looked for foundations other than authority to build a theory of the firm and define a firm’s boundaries. The most influential approach has been the property rights theory of the firm (Grossman and Hart 1986, Hart and Moore 1990, Hart 1995). This theory defines a firm as a set of assets and makes predictions about who should own which assets. Ownership – in this theory – provides bargaining chips to appropriate a larger part of the residual income, which in turn provides incentives to invest. Interpersonal authority plays no role in the property-rights theory.

In addition to responding to the Alchian-Demsetz critique, the property rights theory made two influential methodological contributions: its focus on asset ownership as a characteristic of firms and its insistence on holding the economic environment fixed, i.e., on not simply postulating changes from bringing a transaction inside the firm (Hart 1995, Gibbons 2005). This paper builds on these two methodological contributions of the property rights theory, but returns to the question *why (or whether) bringing an activity inside a firm would give the manager interpersonal authority over the people involved*. In particular, I start from the following three observations: 1) firms hire people under low-powered incentive contracts to work on the firm’s projects (Knight 1921, Simon 1951, Holmstrom and Milgrom 1991), 2) a firm’s manager has interpersonal authority over these employees (Knight 1921, Coase 1937, Simon 1951, Arrow 1974, Williamson 1975), and 3) firms own the assets that are necessary for their activities (Hart 1995, Holmstrom 1999). I will argue that a firm’s centralized

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<sup>1</sup>Along similar lines, Simon (1947) defines authority as follows: ‘A subordinate is said to accept authority whenever he permits his behavior to be guided by the decision of a superior, without independently examining the merits of that decision. When exercising authority, the superior does not seek to convince the subordinate, but only to obtain his acquiescence.’

<sup>2</sup>Note also that these two concepts, while distinct, are closely related: the purpose of interpersonal authority is often to get decision authority, while decision authority often presumes interpersonal authority over the people implementing the decision. While the literature has not always made the distinction explicit – so that I will at times also refrain from making it when discussing earlier literature – the distinction really matters since making people obey is a very different challenge from optimally allocating decision authority.

asset ownership and fixed-wage contracts emerge endogenously as ways to give the firm’s manager interpersonal authority over the firm’s employees. Interpersonal authority and the need to give the manager such authority are themselves equilibrium outcomes of the model. Based on this, I show that the following bundle of practices is optimal:

- All assets that are necessary for one project should be owned by one party. The owner of the project’s assets should also be its residual claimant.
- Other people working on the project should receive low-powered incentives or even fixed wages.
- In equilibrium, the owner tells these employees what to do, and employees obey the owner.

The paper thus provides micro-foundations for the idea that bringing an activity inside a firm gives the manager authority over that activity. I will argue in section 4 that this theory is closely related to Knight’s (1921) theory of entrepreneurship. Note also how this theory relates to earlier approaches and to the Alchian-Demsetz critique: instead of *assuming* that a firm conveys authority, it *explains* the firm as a mechanism to create such authority.

To derive these results, I study a setting in which a number of people can jointly undertake a project. A project is defined as a revenue stream that requires assets and that depends on decisions made by the participants (and potentially on private effort). A key issue is that the participants openly disagree – or have differing priors – on the right decisions, an assumption that I will discuss in more detail later.<sup>3</sup> Decisions are not contractible but the project’s outcome is. Moreover, each player can tell others – through non-binding cheap-talk messages – what he wants others to do. Finally, cooperation is at will: people can walk away from the project. This ability to walk away allows the parties to write efficiency-wage type contracts: by paying more than the market wage, the threat of firing can make one person obey the other. However, the ability to walk away also puts limits on the wages that can realistically be promised. The question is then who should own which assets and write what contracts with whom.

As hinted above, players will – in equilibrium – endogenously create interpersonal authority for one player over others by writing efficiency-wage type contracts (that also make it optimal for that one player to end their contract if the other disobeys). The cheap talk messages will play the role of (non-binding) ‘orders’. The ‘employee’ obeys such non-binding orders because he knows that the contract endogenously commits the owner to firing him if he disobeys and he rather obeys an order which he believes is wrong than to get fired. Note that the role of authority in this paper is to resolve disagreement. This disagreement-resolving role of authority was noted explicitly in Simon’s (1947) observation that ‘[a]n important function of authority is to permit a decision to be made and carried out, even when agreement cannot be reached’ and that ‘when there is disagreement between two persons, and when the disagreement is not resolved by discussion, persuasion, or other means of conviction, then it must be decided by the authority of one or the other participant. It is this “right to the last word” which is usually meant in speaking of “lines of authority” in an administrative organization.’

The intuition behind the paper’s key results is then based on three effects. First, moving asset ownership from the agent to the principal makes it more costly for the agent to get fired, since the agent

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<sup>3</sup>To keep the analysis transparent and completely focused on authority, I will eliminate the possibility of persuasion from the model. This approach should not be interpreted as a claim that firms somehow rely exclusively on authority to get things done. Any firm will rely on both authority and persuasion. And in the end, the choice between authority and persuasion is an economic cost/benefit trade-off and an important issue for further research. The analysis in this and related papers does suggest some conjectures on when firms will choose persuasion over authority: when complementary effort is important, when the agent makes many important similar decisions, and when the power of authority is low (e.g., because the principal cannot commit to firing).

has lower outside options. It also makes it easier for the principal to commit to firing a disobeying agent, since the principal keeps the assets. Both effects give the agent more reason to obey. Asset ownership by the firm thus strengthens the manager's interpersonal authority over the employees. Note that this mechanism depends on how assets affect the *level* of the outside options, as opposed to the slope (with respect to ex-ante investments) which has been the focus of the property rights literature. Second, high-powered incentives give an agent a reason to follow his own beliefs when he disagrees with his principal, and thus lead to disobedience (Van den Steen 2005). As a consequence, low-powered incentives for the employee also increase the manager's interpersonal authority. Finally, the need for interpersonal authority itself derives from the result that it is optimal – under differing priors – to concentrate all control and income of a project in one hand (Van den Steen 2006).

It is important to stress here that interpersonal authority – despite being widely used – poses a real challenge for organizations: a boss's orders often get disobeyed. Such disobedience can come in many forms, such as feigned ignorance, forgetfulness, sloppy work, or even purposeful errors. In his seminal work on organizations, Barnard (1938) wrote, for example, that '(authority) is so ineffective that the violation of authority is accepted as a matter of course and its implications are not considered. It is surprising (...) how generally orders are disobeyed (...).' There is also a drill sergeant's saying that 'The army cannot make you do something, but it sure as hell can make you wish you had.' In the end, people have a free will and it is up to the organization to make them obey. It is for this reason that the need to induce employees to obey orders can indeed be a core determinant of organization design and performance.

I then use this theory of the firm – and build on the insights of Van den Steen (2007a) – to propose the risk of 'break-up' as a new argument for integration. In particular, I show that open disagreement on the right course of action may cause a cooperation or coordination failure in a setting where cooperation or coordination is always optimal from any outsider's perspective. The surprising thing about this coordination failure is that it would persist even if actions were perfectly contractible and bargaining were costless and frictionless, but that it can nevertheless be solved through a change in firm boundaries. The effect of integration is to eliminate disagreement by giving one manager interpersonal authority over all employees. This shows that disagreement may make firm boundaries matter – in a very intuitive way – even when actions are perfectly contractible and there are no incontractible ex-ante investments. (The contractibility part of this result is essentially an application of the ideas in Van den Steen (2007a), which shows that Coase's (1960) examples for the Coase Theorem fail in a differing priors context.) While this cooperation failure is on itself sufficient to make integration strictly optimal, the anticipation of such fundamental disagreement and break-up may furthermore prevent relation-specific investments that require future coordination. Integration will increase specific investments and may then be strictly optimal *even when I allow perfect contractibility of the specific investments and frictionless ex-post bargaining on the decisions*. This also captures the idea that a merger may often dominate an alliance because it provides more control.

The theory in this paper is formulated in terms of a manager-owner or entrepreneur-owner. While this approach has a long tradition – starting with Knight (1921) and Coase (1937) – it obviously raises the question whether the model can be used to study large firms, such as Ford or GE. To answer this question, it is important to point out that the underlying definition of a firm in this paper is that of a firm as a legal person that can write contracts and own assets, as discussed in more detail in subsection 4.1. Since the current paper considers only manager-owned or entrepreneur-owned firms that do not change hands, the firm (as a legal person) and the owner (as a physical person) are interchangeable. There is thus no reason to distinguish them here formally. For transparency reasons, the whole model is therefore (now) formulated in terms of managers-owners. This definition of the firm as a legal entity, however, allows to extend this theory very naturally to a setting of a large firm with a group of shareholders. In particular, as discussed in more detail in section 4, Van den Steen

(2007b) shows that ‘the firm as a legal entity’ effectively aggregates ownership: it allows the manager – despite dispersed firm ownership – to act as the ‘as if’ owner of all assets and thus claim the authority that goes with such centralized ownership (while nevertheless allowing the firm’s owners to maintain checks on the manager’s actions). In other words, the firm as a legal entity allows – in this theory of the firm – risk diversification through broad ownership without losing the benefits of centralized asset ownership for authority.

**Contribution** This paper makes three contributions. First, it shows how asset ownership may convey interpersonal authority, and thus determine effective control. Second, building on this and other results, it shows how a firm’s concentrated ownership and low-powered incentives give the manager interpersonal authority over the firm’s employees. The paper thus provides micro-foundations for the idea that bringing an activity inside a firm gives the manager authority over that activity, while – as part of that – explaining concentrated asset ownership and flat wages as typical characteristics of firms. (An important feature of this theory of the firm is that it can be readily extended to a situation where the firm, as a legal entity, has multiple shareholders. In particular, the firm then aggregates ownership to allow the manager to act as the ‘as if’ owner of all assets and exert the corresponding authority.) Third, it introduces the risk of break-up as a reason for integration. It further shows how the anticipation of such break-up – much like the anticipation of hold-up – may prevent relation-specific investments (even if the investments are contractible, unlike hold-up) and thus lead to integration. These results also illustrate how firm boundaries may matter despite perfect contractibility of investments and actions.

All three contributions, however, are about one thing: how the firm is essentially a mechanism to give the manager interpersonal authority over the firm’s employees.

**Literature** To relate this paper to the literature on the theory of the firm, it is useful to categorize that literature into two groups. The first group are contributions in which interpersonal authority plays no role and ‘the firm’ is just a label for a set of contracts (including property rights). This stream of literature includes, among others, Alchian and Demsetz (1972), the Grossman-Hart-Moore property rights theory, Rajan and Zingales (1998), Levin and Tadelis (2004), and Hart and Moore (2006). The second group are contributions in which interpersonal authority is a key aspect of firms.<sup>4</sup> Early contributions in this group, such as Knight (1921), Coase (1937), Simon (1951), or Williamson (1975), simply asserted such interpersonal authority as fact and directly built on it without much further consideration. Some more recent contributions have focused more explicitly on this authority aspect. In particular, Masten (1988) studied the legal implications of the employment relationship, while Williamson (1991) argued that the doctrine of forbearance denies standing to parties internal to a firm and thus forces their conflicts to be mediated through the hierarchy. These contributions clarify important aspects of authority, but they also leave some important questions open or raise new ones. In particular, Williamson’s (1991) argument is more about the need to rely on authority (as in Holmstrom and Milgrom (1994), which also belongs in this second group but is discussed in more detail below) than about why an employee would obey rather than disobey, while Masten (1988) explicitly states that the legal differences are far from clear-cut and could be replicated by regular market contracting.<sup>5</sup> Furthermore, both contributions are informal in their arguments and don’t relate

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<sup>4</sup>A third group of contributions, such as Hart and Holmstrom (2002), identify firm boundaries with control over decisions without explicitly linking this to interpersonal authority. Such papers would belong in the first group if control is contractible but in the second group when control is determined indirectly through interpersonal authority.

<sup>5</sup>Williamson (1991) also argues that firm and market governance each correspond to a set of internally consistent practices in the sense of Milgrom and Roberts (1990) or Holmstrom and Milgrom (1994). Some of his arguments in this context can potentially be interpreted along the lines of the current paper, such as his statement that ‘workers and

the employee's obedience to firm characteristics such as asset ownership. The difference between the current paper and this second group of literature is that I formally derive the firm – with its centralized asset ownership and low-powered incentives – as *a mechanism to generate* interpersonal authority. In that sense, the paper provides potential formal micro-foundations for this part of the literature. The paper differs from the first group of literature by conceptualizing the firm as a distinct entity – a legal person – and thus not as just a label for a set of contracts, and by its focus on the question what it is about firms that gives a manager ‘interpersonal authority’ over employees or that makes employees obey their manager (i.e., by its focus on the ‘master and servant’ relationship of Coase or on the grocer versus employee issue of Alchian and Demsetz). As further discussed in section 7, the theory of the firm in this paper is highly complementary to most of the existing perspectives on the firm outlined in Gibbons (2005), and at least compatible with the others.<sup>6</sup>

The question how the need to generate interpersonal authority affects organizations was – to my knowledge – first studied in Van den Steen (2005), which shows that pay-for-performance may hinder interpersonal authority, so that interpersonal authority will go together with low-powered incentives or even fixed wages. That paper also shows that people with strong beliefs and high intrinsic motivation will be more likely to become independent entrepreneurs. I discuss the link with the current paper below. In a recent related contribution, Marino, Matsusaka, and Zábajník (2006) study the reverse problem: how organization and market characteristics – such as the agent's job market – affect obedience and thus the equilibrium allocation of control. They do not consider the role of assets or how this feeds into a theory of the firm.

The more specific idea that asset ownership may affect authority has been suggested before, but in a very different sense than the interpretation or formalization in this paper. Hart (1995) mentions the idea that asset ownership can convey authority, but his formalization (p.61) shows that he has something very different in mind than one person giving orders to another person and being obeyed. In particular, Hart shows that asset ownership makes others orient their specific investments towards the asset owner, which he then interprets as asset ownership conveying authority. Holmstrom (1999), in his theory of the firm as a subeconomy, is the first to suggest ideas that are closer to this paper. He argues that ‘asset ownership conveys the CEO (...) the ability to restructure the incentives of those that accept to do business (in or with the firm)’. Ownership then conveys a form of decision authority (over incentives), but not the interpersonal authority that is the focus of this paper. Hermalin (1999) pushes this a step further and argues informally that centralization of control rights may prove difficult without also centralizing asset ownership. In particular, he suggests that if employees own assets, then they can force decisions by threatening holdup or exit. His argument, however, remains very different from the current paper. In particular, the argument in this paper is essentially the reverse: asset ownership by the firm makes the threat of firing the employee both more credible (since the firm retains the assets) and more powerful (since the employee loses the assets and thus has lower outside options), increasing the interpersonal authority of the manager over the employee. Wernerfelt (2002) presents an argument that is a reverse in a different sense: he shows that the person in control – the boss – should own the assets, since he can better internalize the effect of his decisions on the assets.

There are two streams of literature that are closely related to the ideas on interpersonal authority in this paper. The first is the literature on efficiency wages, such as Calvo and Wellisz (1979) or Qian (1994) who consider their effects on hierarchies. While this literature is focused on incentives for effort rather than interpersonal authority and is interested in quite different results, the model

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managers [will] be more willing to accommodate, because their compensation is the same whether they “do this” or “do that”.’ That same statement, however, apparently has interpretations that are completely unrelated to interpersonal authority, making it difficult to relate that discussion to the current paper.

<sup>6</sup>Firms are very complex institutions that cannot be understood from just one perspective to the exclusion of others. For interesting perspectives on this richness, see Holmstrom and Roberts (1998) or Gibbons (2005).

in this paper obviously borrows the idea of an efficiency-wage type setup. The second stream is the literature on relational contracts. Wernerfelt (1997), for example, informally argues that a manager has authority over employees through a relational contract. This raises the question, however, how such relational contracts differ from long-term market relationships or how such authority would get transferred when one firm buys another. It seems that the insights of the current paper on the role of low-powered incentives and asset ownership also apply in that case. The effect of asset ownership should moreover also hold in a standard relational contract setting with common priors, as discussed in section 4. Note, however, that the current paper achieves its authority results without needing to appeal to a repeated-game structure. Note also that this paper differs from Baker, Gibbons, and Murphy (2002) not only by its focus on interpersonal authority, but also by the fact that here the effect of assets is through the *level* of the outside options rather than through the slope with respect to specific investments.

One important feature of this paper is that it simultaneously derives the triple centralized asset ownership, low-powered incentives (or fixed wages), and interpersonal authority as characteristics of firms, and shows how they are closely related. Holmstrom and Milgrom (1994) long preceded this paper with a somewhat similar feature. In particular, they simultaneously explain – by combining monotone comparative statics (Milgrom and Roberts 1990) with multi-tasking (Holmstrom and Milgrom 1991) – the following triple: the firm can exclude employees from certain returns (such as the ability to take outside jobs), employees do not own assets, and employees have low-powered incentives. While excluding employees from certain returns can be done contractually, it can also be done by using authority. When taking that perspective, their paper also deals with the triple asset ownership, low-powered incentives, and authority. One key difference is what is meant with authority: their paper deals with the *use* of authority to forbid employees to receive income from certain activities, while this paper deals with the *origin* of interpersonal authority that is used to *directly* tell employees what to do and what not to do in a fairly general sense. Another important difference is in the role of assets. In Holmstrom and Milgrom (1994), it does not matter who owns the assets, as long as they are not owned by the employee, so that shifting assets from one firm to another does not matter, in contrast to the current paper. This latter distinction is important when it comes to discussing firm boundaries. A key insight of Holmstrom and Milgrom (1994) that has influenced this paper considerably is the observation that low-powered incentives in firms may not simply be an unfortunate consequence but the explicit purpose of transacting through a firm. Their paper is also the first to think about the firm in terms of a set of complementary practices.

The current paper builds on two preceding papers and one parallel paper on contracting under differing priors.<sup>7</sup> Since these papers have close links to the current one, it is important to spell out the contributions in more detail. The two earlier papers have a common origin<sup>8</sup> and deal essentially with the same broad issue: the interaction between disagreement and control in a multi-person project. The first of these papers, Van den Steen (2005), was discussed above. It delivers the result that interpersonal authority will go together with low-powered incentives, which is a key element of the current paper. The second of these papers, Van den Steen (2006), assumes that authority can be allocated contractually and asks how to optimally allocate authority when people may openly disagree. It shows, among other things, that authority over complementary decision should be co-located while authority over substitute decisions should be distributed, and that authority and residual income should be co-located when people have differing priors. The latter result is a key element in the current paper and its intuition will be discussed in more detail later. The parallel paper, Van den Steen (2007a), shows how the Coase Theorem is affected by open disagreement and illustrates how

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<sup>7</sup>A complementary literature, though with different focus, is that on financial contracting under differing priors, such as Boot, Gopalan, and Thakor (2006) or Dittmar and Thakor (2006).

<sup>8</sup>Both papers derive from an earlier working paper ‘Interpersonal Authority: A Differing Priors Perspective’ (2004).

this may lead to a trade failure. This insight on the Coase Theorem is the basis for the result in section 6 of the current paper that the break-up issues persist even when the actions are perfectly contractible through frictionless bargaining. Building on the ideas of the current paper, Van den Steen (2007a) then shows how such trade failure could also be resolved by internalizing the transaction. The contribution of the current paper is to put all these results in a theory-of-the-firm context (with the firm implicitly defined as a legal person), to add asset allocation as another lever, and to show that all this adds up to a theory of the firm and to new implications for firm boundaries.

The following section describes a simple version of the model (which takes the outside options as exogenous and limits the number of assets and players). Section 3 uses that model to derive the key results. Section 4 discusses some important foundations and interpretations of the theory, including the firm as a legal person and the relationship to Knight’s theory of entrepreneurship. Section 5 endogenizes the outside options. Section 6 shows how this theory can explain why the risk of break-up – due to ‘strategic differences’ – may lead to changes in firm boundaries. Section 7 discusses its relationship to other theories of the firm, while section 8 concludes. Some supplementary analysis and less informative proofs are in appendix.

## 2 The Model

The model in this paper captures a setting in which two people can start a project together if they have the necessary assets. The key issue is that the two participants may openly disagree on the right course of action. To resolve this conflict, the participants can try to structure their contract such that one participant effectively controls the other. In particular, one participant can – in the style of an efficiency wage – promise the other a high wage and then threaten to ‘fire’ the other (by ending the contract) if the latter ‘disobeys’. Asset ownership then affects the participants’ outside options when the project is ended prematurely (i.e., when someone gets fired) and thus the control that one player has over the other. In this section, I take the outside options as exogenous to make the analysis maximally transparent. Section 5 will endogenize the outside options by allowing each player to rematch and execute the project with some other player if the first project ends prematurely. (Section 5 will also allow for more players, more projects, and more assets.) The model in this section includes (some) moral hazard and intrinsic motivation, mainly to show that the mechanisms also work in such setting.

Formally, consider two players (denoted  $P_1$  and  $P_2$ ) and two assets (denoted  $a_1$  and  $a_2$ ). The players can engage in a ‘project’, which is a revenue stream  $R$  that requires both players and both assets. As part of this project, each participant  $P_i$  has to make a decision  $D_i \in \{X, Y\}$ .<sup>9</sup> One and only one of these choices is correct, as captured by the state variable  $S \in \{X, Y\}$ , which happens to be common to both decisions (although that is not necessary for the results).<sup>10</sup>

As depicted in figure 1, the project will be either a success or a failure. A failure always gives payoff  $B > 0$ , while a success gives payoff  $B + 1$  with probability  $\eta$ , and  $B$  otherwise. This probability  $\eta$  will depend on the players’ effort, as discussed later.<sup>11</sup> The probability of success itself, denoted by  $Q$ , depends on which decisions are correct. In particular, let  $d_i = I_{\{D_i=S\}}$  be the indicator that  $P_i$ ’s decision  $D_i$  is correct and let the probability of success be  $Q(d_1, d_2) \in [0, 1]$ , with  $Q$  symmetric and

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<sup>9</sup>One can think of the two players as the production/engineering person and the marketing/sales person. The decision may be, for example, high quality versus low cost strategy.

<sup>10</sup>In particular, in section 6 the states will be decision-specific.

<sup>11</sup>This moral hazard is not at all necessary for the analysis. It is introduced merely to show that the model works in a setting with moral hazard. (In particular, I will also show the results for  $\eta \equiv 1$  independent of any effort.) The same holds for the role of intrinsic motivation, i.e., of private benefits from success, discussed later.

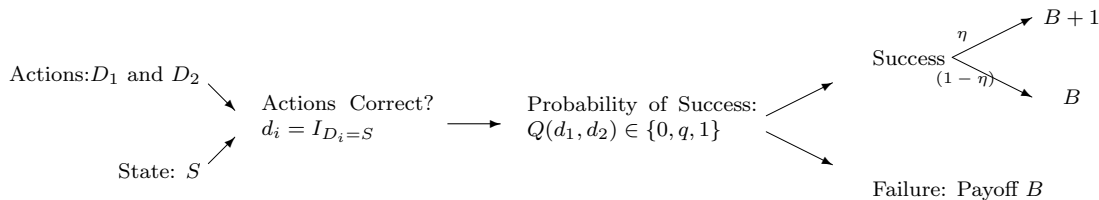


Figure 1: Actions and Payoffs

1	2	3	4
Contracting	Orders and Decisions	Execution	Payoffs
<ul style="list-style-type: none"> <li>a The players negotiate contract <math>(v_i, \alpha_i, F_i)</math> (via Nash bargaining).</li> <li>b <math>F</math> is paid instantly.</li> <li>c The beliefs <math>\mu_i</math> get (privately) drawn.</li> </ul>	<ul style="list-style-type: none"> <li>a Each player can send a cheap-talk message from <math>\{X, Y\}</math>.</li> <li>b Each player publicly chooses his action from <math>\{X, Y\}</math>.</li> <li>c With probability <math>p</math>, each player can end the contract (prior to stage 3), in which case each <math>P_i</math> gets his outside option <math>\underline{u}_i</math>.</li> </ul>	<ul style="list-style-type: none"> <li>a Success or failure is revealed, assets are committed.</li> <li>b Each player can end the contract, in which case each <math>P_i</math> gets his outside option 0.</li> </ul>	<ul style="list-style-type: none"> <li>a The players choose simultaneously whether to exert effort.</li> <li>b The contract terms <math>(v_i, \alpha_i)</math> get executed.</li> </ul>

Figure 2: Time line of basic model

strictly increasing in  $d_1$  and  $d_2$ ; and with  $Q(0, 0) = 0$ ,  $Q(1, 1) = 1$ , and  $Q(0, 1) = Q(1, 0) = q \in (0, 1)$ .

The state  $S$  is unknown, but each player  $P_i$  has a subjective belief  $\mu_i$  that  $S = X$ . A key assumption is that (it is common knowledge that) players have differing priors, i.e., they can disagree in their beliefs about  $S$  even though neither player has private information about  $S$ . I will discuss this differing priors assumption in more detail at the end of this section. The fact that players may have differing priors about  $S$  and that there is no private information implies that players will not update their beliefs when they notice that someone else has a different belief: they simply accept that people sometimes disagree.

To keep the analysis simple, both players' beliefs will be independent draws from a commonly known binary distribution: for some  $\nu \in (.5, 1)$ ,  $\mu_i$  equals  $\nu$  or  $(1 - \nu)$  with equal probability. This implies that  $i$  believes half the time that  $X$  is the best course of action, and half the time that  $Y$  is the best course of action. But  $i$  always has the same confidence (or strength of belief in what he believes is best)  $\nu = \max(\mu_i, 1 - \mu_i)$ . Moreover, the two players disagree half the time. In the main analysis, both players have the same confidence  $\nu$  in order to make clear that the results are not driven by asymmetries between the players. I will, however, also consider what happens when players may differ in their level of confidence  $\nu_i$ .

The timing of the game is indicated in figure 2. First, the players negotiate a contract via symmetric Nash bargaining, with outside values as described later.<sup>12</sup> To discuss the contract, I need to specify what is contractible and what is not. I will assume that the decisions  $D_i$  (in stage 2b) are not contractible, and neither the right to make these decisions. However, the project success *is* contractible. A contract will then consist of a fixed payment  $v_i$ , a share  $\alpha_i \in [0, 1]$  of the extra project revenue upon success, and an up-front transfer  $F_i$ . For budget balance reasons, we need  $v_1 + v_2 = B$ ,  $\alpha_1 + \alpha_2 = 1$ , and  $F_1 + F_2 = 0$ . The restriction  $\alpha_i \in [0, 1]$  is in fact a no-wager condition: absent this condition, the

<sup>12</sup>Alternatively, the outside options could also be zero or some other fixed values. Logically, however, the outside value at this point should be at least as high as the one later in the game. The paper's setup is the simplest way to ensure this. There are also many variations on this bargaining procedure that would work, such as take-it-or-leave-it offers in a random or fixed sequence or asymmetric Nash bargaining.

players would bet on the state and – in doing so – generate infinite utility. This no-wager condition can be derived endogenously by giving each player the ability to sabotage the project, i.e., by giving each player the ability to make sure that the project fails (Van den Steen 2005). In that case, any contract with  $\alpha_i \notin [0, 1]$  would give one of the players a strict incentive to sabotage the project. Anticipating that, the other would never accept the ‘bet’. To maintain generality and to simplify the analysis, I simply impose the condition as an assumption. In stage 1c, the players’ beliefs get privately realized.<sup>13</sup>

In stage 2a, each player can send a cheap talk message from the set  $\{X, Y\}$  to the other player. (As will become clear in section 3, in equilibrium only one party – the boss – will send a cheap-talk message and it will be interpreted by the other party – the subordinate – as a non-binding order.) In order to exclude non-interesting cheap talk equilibria, I will assume that the players select the Pareto-dominant equilibrium if one exists. Moreover, while sending messages is costless, I assume that players have a lexicographic preference for being obeyed: when they are payoff-indifferent, they will send a message only if it is strictly more likely to be obeyed than to be disobeyed. In step 2b, the players publicly choose their actions. Since the players’ decisions are non-contractible, each agent always chooses the decision that is best from his perspective, given his beliefs and the contract negotiated in stage 1. (In this sense, an order from the boss does not directly constrain the subordinate’s behavior.)

After the actions, players can end the contract, and this comes in two forms. First (in step 2c), with small probability  $p$ , both players have the chance to end the project before the assets are committed. Then (in step 3b), after the assets are committed and the project outcome is revealed (in step 3a), players for sure get the chance to end the contract. (As will become clear in section 3, the ability to terminate the contract will allow one player to effectively ‘fire’ the other, although it will only take on that meaning in equilibrium. At this point, both players are symmetric.)

If either player ends the contract in step 2c, then the project is over and each player  $P_i$  gets his outside option  $\underline{u}_i$ . Player  $P_i$ ’s outside option will depend on the set of assets he owns (denoted  $A_i$ ). Let  $P_i$ ’s outside option then be denoted  $\underline{u}_i(A_i)$  and assume that both players’ outside options depend in the same way on the set of assets they own, i.e.,  $\underline{u}_i(A) = \underline{u}(A)$ . In this section, I take the outside options as exogenous. I will assume, first of all, that  $\underline{u}(\emptyset) = 0$ ,  $\underline{u}(\{a_1\}) = \underline{u}(\{a_2\}) > 0$ , and  $\underline{u}(\{a_1\}) + \underline{u}(\{a_2\}) = \underline{u}(\{a_1, a_2\}) \equiv \underline{u} < B + \nu$ . All these conditions will arise naturally when the outside options are endogenized – as in section 5 – as future opportunities to match and execute the project with other players. I will furthermore assume that  $\underline{u}(\{a_1, a_2\}) > B + q$ , which I will derive in section 5 from a more primitive assumption (on the discount factor). I will discuss the meaning and role of this assumption at that time. If either player ends the contract in stage 3b, then the game is over and both players get their outside option, which is now 0 (since  $A_i = \emptyset$ ). I will assume that  $p < 2 - \frac{1}{\nu}$ . This assumption will have the effect to limit the probability that the principal can fire the agent prior to the assets being committed, which will then give the agent a temptation to disobey.

In period 4a, both players can exert effort. As mentioned earlier, such effort affects the probability  $\eta$  that a success gives a payoff  $B + 1$  rather than  $B$ . In particular, I will assume that  $\eta = 1$  if both players exert effort and  $\eta = \theta$  otherwise. Effort carries a private cost  $e$  for each player. I will again consider only Pareto-optimal outcomes.<sup>14</sup> In period 4b, finally, the payoffs are realized and the

<sup>13</sup>These belief realizations can be interpreted as the beliefs after the players have exhausted all economic means of persuasion. In particular, if – as is often the case in strategic or acquisition decisions – all players have access to the same information and further data collection is extremely costly (since this is a once-and-for-all decision and the only possible experiment is to execute the project), the beliefs they form are the posteriors that become the priors for this game and will thus be used to make decisions. The meaning of the differing priors assumption is discussed further at the end of this section.

The beliefs being drawn after the contract is signed captures the idea that the contentious issues become clear only after the project is started. So one could imagine that there are an infinite number of potential issues (on which each player has given beliefs), and stage 1c reveals which of these issues is the one that matters for this project.

<sup>14</sup>In this case, any sequencing of the effort choices will automatically lead to the Pareto-optimal outcome.

contract terms  $(v_i, \alpha_i)$  get executed. Apart from their share in the residual income, both players also get a private benefit from a high payoff  $\gamma \geq 0$ , which captures intrinsic motivation.<sup>15</sup>

The reason to introduce – in stage 4 – moral hazard and intrinsic motivation is not to study their effect in full generality but rather to show that the interpersonal authority results of the model are robust to some amount of moral hazard and intrinsic motivation. I will therefore put explicit limits on their importance to keep the analysis simple. I distinguish two cases. The first case is one where moral hazard plays no role. In particular, with  $\epsilon = \min(B + \nu - \underline{u}, \underline{u} - B - q, B) > 0$ , the first case consists of the following assumption:

**Assumption 1a**  $\theta = 1$  and  $\gamma \leq \frac{pe}{4}$

The second case is when moral hazard is non-trivial, which consists of the following assumption:

**Assumption 1b**  $0 < (1 - \theta) \leq \frac{\epsilon}{2}$ ,  $e \leq \frac{(1-\theta)^2}{2}$ , and  $\gamma \leq \frac{pe}{(1-\theta)}$ .

where  $\gamma \leq \frac{pe}{(1-\theta)}$  implies the earlier  $\gamma \leq \frac{pe}{4}$ . Unless explicitly mentioned, I will consider the second case, with the moral hazard issues.

To summarize, there are essentially two sets of moving parts in this model, each with a clear purpose. The first set enables interpersonal authority to play a role: the drawing of beliefs (so that there is something to give orders about), the cheap talk messages (so that an order can be given), and the decisions (so that the other can either obey or disobey). The second set enables the efficiency wage: the contracting up-front (so that they can agree on a wage), the ability to quit (so that the principal can fire the agent), and the outside options.

The purpose of the analysis is to determine the allocation of assets – and the equilibrium that goes with it – that will maximize the joint utility of all players,  $U$ . In doing so, I will consider only pure-strategy subgame-perfect equilibria that are not Pareto dominated. Such equilibria always exist.<sup>16</sup> I will also consider whether the allocation would be different if the assets were traded or auctioned off at the start of the game.

**The Differing Priors Assumption** The model assumes that people can openly disagree, i.e. they have differing priors.<sup>17</sup> While I consider the role of this assumption in section 4, I discuss it here from a more general perspective.

Note first that the differing priors assumption is not in any way new. Earlier papers with this assumption include, among others, Arrow (1964), Wilson (1968), Harrison and Kreps (1978), Leland (1980), Varian (1989), Harris and Raviv (1993), Morris (1994, 1997), Daniel, Hirshleifer, and Subrahmanyam (1998), Scheinkman and Xiong (2003), Yildiz (2003, 2004), Van den Steen (2004b), Brunnermeier and Parker (2005), Boot, Gopalan, and Thakor (2006), and Guiso, Sapienza, and Zingales (2006). There has been a rapid rise in recent years, in part due to the growing popularity of

<sup>15</sup>Note that with  $\gamma > 0$ , we need a further modification – beyond the ability to sabotage – to endogenize the condition  $\alpha \in [0, 1]$  (because sabotage alone would give you  $\alpha \in [-\gamma, 1 + \gamma]$ ). A probabilistic structure for  $\gamma$  would do. Consider, for example, the case that  $\gamma = 0$  with probability  $s$  and  $\gamma = \hat{\gamma}$  with probability  $1 - s$ . Any  $\alpha \notin [0, 1]$  would then lead to sabotage with at least probability  $s$ .

<sup>16</sup>The focus on pure-strategy equilibria that are not Pareto dominated excludes only equilibria that are extremely similar to the ones I obtain here (where, for example, a player doesn't quit for sure, but with 'sufficiently high probability') and equilibria that are not very realistic or not very interesting (where, for example, both players quit simply because the other quits and therefore they are indifferent between quitting or not).

<sup>17</sup>Obviously, the assumption in this paper that players have absolutely no private information is extreme and made for analytical convenience. If players had both differing priors and private information, they would update their beliefs when encountering someone with whom they disagree, but disagreement would remain (Morris 1997).

For a more conceptual discussion of differing priors, see Morris (1995). Note that differing priors is *not* the same as private information that is impossible to communicate.

behavioral economics which often implicitly assumes differing priors. There is also a burgeoning empirical literature such as Chen, Hong, and Stein (2002) or Landier and Thesmar (2007). Furthermore, Hong and Stein (2007) argue that ‘disagreement models (...) represent the best horse on which to bet [as the future consensus model for behavioral finance].’

The assumption of (originally unbiased) differing priors captures the fact that people may have different ‘mental models’ or ‘belief systems’ or different intuition. Such different mental models or intuition may lead people with identical data to draw different conclusions. Consider, for example, one’s belief whether to trust a particular person or a particular group of people, or one’s belief to trust intuition over data, or one’s belief whether fear is a good motivator, how close we are to a tipping point in climate, or whether we will be watching television on our cell phones. Such beliefs have immediate implications for business decisions. Whether to delegate a set of decisions to the assembly line workers depends on whether you trust these workers. The HP-Compaq merger depended on one’s belief whether the ‘old HP’ with the ‘HP way’ could flourish as a global corporation. Product design and R&D investment decisions for cell phones depend critically what you believe people will be using cell phones for 5 years down the road. These kinds of issues are repeated many times over in organizations. People disagree on how to design an organization, on how to deal with a difficult employee, on whether to trust a supplier, etc. (While the model in this paper is written as being about one issue, it is not difficult to rewrite it as being about a succession of smaller issues.) Open disagreement is thus an issue in both strategic and day-to-day decision making. In effect, the fundamental role of ‘belief systems’ or ‘mental models’ in organizations has been stressed by academic studies of managers and managerial decision making (Donaldson and Lorsch 1983, Schein 1985).

An important question is why – if the decision is important – players don’t simply discuss until they reach agreement. The answer is that the choice between persuasion and authority is a time and cost trade-off, and in many cases persuasion is just not the right option. In particular, many of these beliefs are deeply engrained and difficult to change, while further data collection may be costly and time consuming. Consider, for example, the case that you disagree on whether to trust a group of employees sufficiently to delegate certain decisions to them. It is very difficult to rationally persuade someone to really trust another person when they are not already inclined to do so. Moreover, further data collection to resolve this disagreement is complex and probably very time-consuming. Finally, the process of convergence of beliefs is more complex than it may seem at first sight.<sup>18</sup> It may then be much more effective to rely on authority to simply order the other to delegate these decisions. As shown in this paper, such authority may sometimes be relatively cheap to implement. To see this from another perspective, imagine the deadlock if a CEO (or a Dean) needed to persuade all his subordinates every time of the correctness of his judgment before making a decision, or if a board could only decide by *true* unanimity of opinions! Overall then, the possibility of persuasion will not eliminate the need to study disagreement, and how to resolve it by authority.

A final question is where such differing priors would come from in a Bayesian framework? There are two ways to think about this. Since the prior for this game is a posterior from earlier updating, (unconscious) bounded rationality will often lead to differing priors, even when starting from a common prior. Unconsciously forgetting some of the data used to update beliefs, for example, would do. A second – more philosophical and more controversial – argument is that people may be born with

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<sup>18</sup>While in most cases, more data tend to lead to convergence, this is definitely not guaranteed. There are indeed both empirical (Lord, Ross, and Lepper 1979, Plous 1991, McHoskey 1995) and theoretical (Diaconis and Freedman 1986, Acemoglu, Chernozhukov, and Yildiz 2006) reasons why that may not be the case. Acemoglu, Chernozhukov, and Yildiz (2006) show, for example, how potential disagreement over the interpretation of new information is sufficient to prevent convergence. The psychology literature on polarization shows empirically how differential reading of identical information may sometimes lead to divergence. This does not mean that convergence will not happen, only that it is a more difficult process than often imagined. This will particularly be the case when the disagreement derives from different ‘mental models’ or ‘world views’, since these often imply different interpretation of data.

differing priors: in the absence of information there is no reason to agree. From that perspective, differing priors are perfectly consistent with a fully rational Bayesian paradigm: priors are just primitives of a model. In this paper, I am completely agnostic about the source of the disagreement. I just believe that disagreement can be an important force in organizations and explore its potential consequences.

### 3 Interpersonal Authority, Ownership, and Contracts

This section derives the main results of the paper. In particular, it shows that the optimal asset allocation is such that all assets required for the project are owned by one party; that the owner then hires others under a low-powered or fixed-wage contract to work on the project; and that these ‘employees’ take orders from the owner.

Before going to the formal analysis, let me give an overview of the different forces at work. As is clear from section 2, the unit of analysis is a project: a revenue stream that requires assets and depends on decisions. A basic result of the earlier literature is that – with differing priors – it is optimal to concentrate all income and control rights of a project in one hand (Van den Steen 2006): as a person gets more control rights, she values (by revealed preference) income rights higher, so it is optimal to give her more income rights; as a person gets more income rights, she values control rights higher, making it optimal to give her more control rights.<sup>19</sup>

With income rights perfectly contractible, the issue is how to also move control rights around. As mentioned before, the approach will be to use an efficiency-wage type scheme: one player promises the other a high wage, tells him what to do, and threatens to fire him if he disobeys. To make this work, the principal must make sure not only that getting fired is costly to the agent, but also that he himself is committed to firing a disobeying agent. If not, he may be faced with the well-known situation of an obstructive employee who knows he can’t get fired.

The rest of the analysis is about two mechanisms that strengthen interpersonal authority in such an efficiency-wage type context. The first mechanism – based on Van den Steen (2005) – is that by giving the agent low-powered incentives, such as a fixed wage, the principal minimizes the agent’s temptation to disobey the principal when the two of them disagree on the right course of action.

The second mechanism to strengthen the manager’s interpersonal authority is through the allocation of asset ownership. Following the property rights theory, a key characteristic of ownership is residual control over the assets: when cooperation breaks down, ownership determines who gets the assets and thus what the level of each player’s outside option will be. On their turn, the level of these outside options determine the cost of firing and getting fired, and thus the agent’s incentives to obey the principal. There are actually two effects. First, if an employee owns an asset that is critical to the firm, then the firm will think twice before firing him and the employee will know that and use it. Second, the employee will care less about getting fired when he owns the asset since he has better outside options. The opposite is true when the firm owns all the relevant assets: the employee will feel both replaceable and vulnerable, and will thus be quick to please his boss.

I will now derive these results formally. Since interpersonal authority is such an important part of the analysis, I will first derive the conditions under which one participant obeys the other. To that end, I will study the subgame that starts in 2a – thus taking the asset allocation and the compensation contract  $(\alpha_i, v_i)$  as given – and consider under what conditions one player will do what the other tells him to do. To simplify some of the notation, I will assume that the players are renamed such that  $P_1$

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<sup>19</sup>As argued in Van den Steen (2006), this *intuition* is specific to differing priors. First, with common priors, all players value residual income identically (in expectation). Second, an increase in a player’s share of residual income does not, in itself, make him value control more in a context with common priors: it just makes him care more about making sure that the person with the most information gets to make the decision, whoever that is.

physically gets the income of the project and pays  $P_2$  a wage  $w$  and a share  $\alpha$  of the extra revenue upon success, so  $\alpha_1 = (1 - \alpha)$  and  $\alpha_2 = \alpha$ . (Since this is just notation, it will not affect the results.) I will furthermore use  $Z_i$  to denote the action that player  $P_i$  believes is most likely to succeed;  $U$  to denote the joint expected utility of both players. Note that the expected project payoff according to player  $P_i$  when  $Z_i$  was implemented for both decisions is  $\nu$ , while the expected project payoff according to  $P_i$  when  $Z_i$  was implemented for one decision but not for the other is  $q$ .

The following lemma describes the pure-strategy equilibria of the game (that are not Pareto dominated), starting in stage 2. I will use ‘Authority by  $P_i$ ’ to denote the following equilibrium outcome:  $P_i$  orders  $P_j$  what to do;  $P_j$  obeys  $P_i$ ’s orders;  $P_i$  ends the contract (i.e., ‘fires’  $P_j$ ) if  $P_j$  were to disobey;  $P_i$  himself chooses  $Z_i$ ; and neither player quits in equilibrium. I will use ‘No Authority-Stay’ to denote the following equilibrium outcome: neither player orders the other what to do, each player  $P_i$  chooses  $Z_i$ , and both players stay. If will, finally, use ‘No Authority-Quit’ to denote the following equilibrium outcome: neither player orders the other what to do, each player  $P_i$  chooses  $Z_i$ , and one or both players end the contract when they turn out to disagree. The following lemma then states all possible equilibria where the project gets executed and no player quits for sure. To state the lemma, let  $\tilde{\alpha}_i = (\alpha_i + \gamma) - e$  if  $\min_i(\alpha_i + \gamma)(1 - \theta) \geq e$ ;  $\tilde{\alpha}_i = (\alpha_i + \gamma)\theta$  otherwise; and  $\kappa = (1 - p)/p$ .

**Lemma 1** *There exist only 4 pure-strategy (subgame) equilibria that are not Pareto dominated:*

1. ‘Authority by  $P_1$ ’ if  $w \in [\max(B + \tilde{\alpha}_1 q - \underline{u}_1, \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2), \min(B + \tilde{\alpha}_1 \nu_1 - \underline{u}_1, B)]$ , which gives  $U_{Au-1} = B + \tilde{\alpha}_1 \nu_1 + \tilde{\alpha}_2 \frac{1}{2}$ ,
2. ‘Authority by  $P_2$ ’ if  $w \in [\max(-\tilde{\alpha}_2 \nu_2 + \underline{u}_2, 0), \min(-\tilde{\alpha}_2 q + \underline{u}_2, B - \tilde{\alpha}_1(\kappa(2\nu_1 - 1) - (1 - \nu_1)) - \underline{u}_1)]$ , which gives  $U_{Au-2} = B + \tilde{\alpha}_2 \nu_2 + \tilde{\alpha}_1 \frac{1}{2}$ ,
3. ‘No Authority-Quit’ if  $w \in [\max(-\tilde{\alpha}_2 \nu_2 + \underline{u}_2, B + \tilde{\alpha}_1 q - \underline{u}_1, 0), \min(B + \tilde{\alpha}_1 \nu_1 - \underline{u}_1, \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2, B)]$  or if  $w \in [\max(-\tilde{\alpha}_2 \nu_2 + \underline{u}_2, B - \tilde{\alpha}_1(\kappa(2\nu_1 - 1) - (1 - \nu_1)) - \underline{u}_1, 0), \min(-\tilde{\alpha}_2 q + \underline{u}_2, B + \tilde{\alpha}_1 \nu_1 - \underline{u}_1, B)]$  which gives  $U_{NAu-Quit} = \frac{B + \tilde{\alpha}_1 \nu_1 + \tilde{\alpha}_2 \nu_2}{2} + p \frac{\underline{u}_1 + \underline{u}_2}{2} + (1 - p) \frac{B + (\tilde{\alpha}_1 + \tilde{\alpha}_2)q}{2}$ .
4. ‘No Authority-Stay’ if  $w \in [-\tilde{\alpha}_2 q + \underline{u}_2, B + \tilde{\alpha}_1 q - \underline{u}_1] \cap [0, B]$ , which gives  $U_{NAu-Stay} = B + \frac{\tilde{\alpha}_1 \nu_1 + \tilde{\alpha}_2 \nu_2 + (\tilde{\alpha}_1 + \tilde{\alpha}_2)q}{2}$ .

**Proof :** See appendix. ■

The proof of the lemma is in appendix since doing the full backwards induction is uninstrucive and quite tedious. Moreover, the basic intuition can be readily understood from looking at the different sets of conditions. Consider first the conditions for ‘Authority by  $P_1$ ’:  $w \geq B + \tilde{\alpha}_1 q - \underline{u}_1$  or  $\underline{u}_1 \geq B + \tilde{\alpha}_1 q - w$  commits  $P_1$  to firing  $P_2$  when the latter disobeys<sup>20</sup>,  $w \geq \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2$  derives from  $\tilde{\alpha}_2(1 - \nu_2) + w \geq p\underline{u}_2 + (1 - p)(\tilde{\alpha}_2 \nu_2 + w)$  which makes it incentive compatible for  $P_2$  to obey if  $P_1$  fires him otherwise, while  $w \in [0, \min(B + \tilde{\alpha}_1 \nu_1 - \underline{u}_1, B)]$  makes it ex-ante and ex-post individually rational to participate in the project. The conditions for the ‘No authority-Stay’ case guarantee that neither player will quit if the other disobeys (as long as he himself makes the decision that he considers best), while the conditions for the ‘No authority-Quit’ case guarantee that each player will do as he likes (even if the other quits upon disobedience) and that players quit if and only if they disagree.

I now turn to the main result of this paper, i.e., the result on ownership, low-powered incentives, and interpersonal authority. To state this result formally, let  $O_{ij}$  denote the ownership structure where asset  $a_1$  is owned by  $P_i$  and asset  $a_2$  is owned by  $P_j$ , with potentially  $i = j$ . Let  $\omega = (\nu, \gamma, e, \theta, \underline{u})$  be a set of parameters excluding  $p$  and let  $\hat{\Omega}$  denote the set of parameters  $(\omega, p)$  that satisfy all the assumptions of the model, including assumption 1b.

<sup>20</sup>This is somewhat similar to the role of wages in Kahn and Huberman’s (1988) model of up-or-out contracts.

The following proposition then says that allocating both assets to one player is the only ownership allocation that maximizes the joint expected utility  $U$  for all parameter values. Moreover, the only equilibrium that then maximizes  $U$  is such that: residual income gets allocated as much as possible to the owner; the owner hires others under a contract that either pays a fixed wage or, sometimes, the minimal incentives to get the employee to exert effort; the owner orders these other players what to do; and they obey. In other words, owners hire non-owners as employees, and these employees take their orders from the owner. I will discuss some more of the intuition after the proposition.

**Proposition 1** • *An ownership allocation  $O$  maximizes  $U$  for all  $B$  iff  $O \in \{O_{11}, O_{22}\}$ .*

- *When the ownership structure is  $O_{ii}$ , the unique equilibrium is  $Au-P_i$ .*
- *Under assumption 1a, the contract in this equilibrium sets  $\hat{\alpha} = 0$  and  $w = \gamma(\kappa(2\nu_2 - 1) - (1 - \nu_2))$ .*
- *Under assumption 1b, for any  $\omega$ , there exists some  $\tilde{p} < 2 - \frac{1}{\nu_2}$  such that the contract in this equilibrium is as follows:*
  - *for  $p < \tilde{p}$  and  $(\omega, p) \in \hat{\Omega}$ , the contract sets  $\hat{\alpha} = 0$  and  $w = \gamma(\kappa(2\nu_2 - 1) - (1 - \nu_2))$ , and neither player exerts effort,*
  - *for  $\tilde{p} \leq p < 2 - \frac{1}{\nu_2}$  and  $(\omega, p) \in \hat{\Omega}$ , the contract sets  $\hat{\alpha} = \frac{e}{(1-\theta)} - \gamma$  and  $w = \frac{e}{(1-\theta)}(\kappa(2\nu_2 - 1) - (1 - \nu_2))$ , and both players exert effort.*

**Proof :** Let  $\hat{U}_e$  and  $\hat{U}_{ne}$  denote the maximal joint (expected) utility of an authority equilibrium with and without effort and  $\hat{U}_{NAu}$  the maximal joint utility of the respective no-authority equilibrium. The proof of lemma 1 then showed that in the absence of  $w$ -feasibility constraints,  $\hat{U}_{ne} > \max(\hat{U}_{NAu-Stay}, \hat{U}_{NAu-Quit})$  and (in the case with moral hazard, i.e., assumption 1b)  $\hat{U}_e > \hat{U}_{ne}$ . The first inequality implies that it suffices to show that  $\hat{U}_{ne}$  is always feasible to conclude that any equilibrium must be  $Au-P_i$ .

To show that  $\hat{U}_{ne}$  is always feasible, consider  $O = O_{11}$  (so that  $\underline{u}_1 = \underline{u}$  and  $\underline{u}_2 = 0$ ). An  $Au-P_1$  equilibrium then requires that

$$w \in [\max(B + \tilde{\alpha}_1 q - \underline{u}, \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2))), \min(B + \tilde{\alpha}_1 \nu_1 - \underline{u}, B)]$$

Since  $B + \tilde{\alpha}_1 q < \underline{u}$  and  $\kappa(2\nu_2 - 1) - (1 - \nu_2) > 0$ , increasing  $\alpha_1$  increases the  $w$ -interval in the strong set-order (i.e., intervals at lower values are subsets of the intervals at higher values). Since increasing  $\alpha_1$  thus both increases the objective ( $U_{Au-1}$ ) and loosens the constraint, any  $Au-P_1$  equilibrium must have either  $\alpha_1 = 1$  (with neither player exerting effort) or  $\alpha_1 = 1 - \left(\frac{e}{(1-\theta)} - \gamma\right)$  (with both players exerting effort). For further reference, the fact that  $\hat{U}_e > \hat{U}_{ne}$  (in the case with moral hazard) implies that an  $Au-P_i$  equilibrium will have both players exerting effort whenever such effort equilibrium is feasible. To show now that  $\hat{U}_{ne}$  is always feasible, note that the  $Au-P_1$  equilibrium without effort thus requires  $w \in [\gamma(\kappa(2\nu_2 - 1) - (1 - \nu_2)), \min(B + (1 + \gamma)\nu_1 - \underline{u}, B)]$ . Given the assumption that  $\gamma \leq \frac{pe}{4}$ , this condition can always be satisfied by  $w = \gamma(\kappa(2\nu_2 - 1) - (1 - \nu_2))$ , so that ‘ $Au-P_1$  without effort’ with  $\alpha_1 = 1$  is indeed always feasible. It also follows that the (optimal) equilibrium must always be an  $Au-P_i$  equilibrium (since any  $NAu$  equilibrium is dominated by a feasible equilibrium). This establishes the second and third points of the proposition and also reduces the overall problem to finding the optimal  $Au-P_i$  equilibrium.

I concluded above that the  $Au-P_i$  equilibrium will have both players exerting effort whenever the  $w$ -condition of such equilibrium can be satisfied. By symmetry, I can limit attention to  $Au - 1$ . Note that shifting assets to  $P_1$  will relax the  $w$ -condition. The  $w$ -condition for an equilibrium with effort thus requires

$$w \in \left[ \left( \frac{\theta e}{(1-\theta)} \right) \left( \frac{(1-p)}{p} (2\nu_2 - 1) - (1 - \nu_2) \right), \min \left( (1 + 2\gamma - \frac{2-\theta}{(1-\theta)} e) \nu_1 + B - \underline{u}, B \right) \right]$$

Since  $\frac{(1-p)}{p} (2\nu_2 - 1) - (1 - \nu_2) > 0$  (by the assumption that  $p < 2 - \frac{1}{\nu_2}$ ), since  $\lim_{p \uparrow (2 - \frac{1}{\nu_2})} \frac{(1-p)}{p} (2\nu_2 - 1) - (1 - \nu_2) = 0$ , and since  $\lim_{p \downarrow 0} \frac{(1-p)}{p} = \infty$ , there exists some  $\tilde{p}$  such that the  $Au-P_1$  equilibrium with effort is feasible only when  $p \geq \tilde{p}$ . This implies the fourth part of the proposition.

All that is left to show is that only  $O \in \{O_{11}, O_{22}\}$  maximize  $U$  for all  $B$ . To see this, consider  $O = O_{ij}$  with  $i \neq j$  and  $B \leq \frac{u}{2}$ . The feasibility condition for  $Au-P_1$  (which was shown above to be the only equilibrium that maximizes  $U$ ) is then

$$w \in \left[ \max \left( B + \tilde{\alpha}_1 q - \frac{u}{2}, \tilde{\alpha}_2 (\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \frac{u}{2} \right), \min \left( B + \tilde{\alpha}_1 \nu_1 - \frac{u}{2}, B \right) \right]$$

which is impossible with  $B \leq \frac{u}{2}$  since that implies  $B < \tilde{\alpha}_2 (\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \frac{u}{2}$ . This completes the proposition.  $\blacksquare$

This proposition thus delivers the results on ownership, low-powered incentives, and interpersonal authority. While most of the intuition for these results was discussed earlier, there are a few further points that are worth mentioning. First of all, note that no player can credibly promise a wage that exceeds  $B$ , since each player can end the contract after the state realization. This wage limitation plays a significant role. In particular, if there were truly no limit on the wage you can promise, then you can always get obedience by promising an infinitely high wage and threatening to fire upon disobedience. Such extremely high wage, however, creates problems when the project fails and generates much less income than the wage that is due. In that event, the party owing the (extremely high) wage will use all possible means to try to get out of the contract, e.g., by trying to fire the employee for cause or by arguing that the wage is not proportional to the employees' services and thus illegal. That is what the model's assumption captures.<sup>21</sup>

Second, while the discussion has focused on the need to create authority, note that the co-location of residual income and residual control also favors shifting the assets to the person in control and using low-powered incentives. In particular, the person who owns an asset must be compensated for its use (because otherwise he ends the project and takes the outside option). When the required compensation exceeds the feasible wage, then part of that compensation must be paid as a share of residual income. Ownership of assets by someone who is not in control thus also allocates residual income away from the person in control, which I argued to be inefficient: the person in control has a higher valuation of the residual income (by revealed preference) so it is efficient to allocate residual income as much as possible to him. This observation does raise the possibility that the asset concentration and low-powered incentives are caused by the latter effect rather than by the need for authority. The way to distinguish the two effects is by comparing the original model to a benchmark model in which obedience is simply contractible. Appendix B analyzes exactly this comparison and confirms that the need for authority indeed increases the need for low-powered incentives and for concentrated asset ownership.

I now consider three important variations on the main model: the case where people may have different confidence levels  $\nu_i$ , the case of endogenous asset allocation, and the case where moral hazard is really important. The latter two are only discussed informally.

**Heterogeneity in Confidence Levels** People often differ in their confidence regarding particular issues or projects. For any issue, from the evolution of the stock market to the scientific validity of classroom experiments, there are people with strong views and people with weak views. How would such heterogeneity affect the predictions of the model? Intuitively, it seems that people with strong views will tend to be in charge: since they have strong beliefs what to do with the project, they value control highly. They can also relatively easily commit to firing disobeying employees. People with

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<sup>21</sup>Introducing a cost for ending the contract would not affect the results. Note also that there are other sets of assumptions that would generate the results of the paper. One example is a setting where the (completely binding) contract specifies payments conditional on the three possible outcomes (failure with asset uncommitted, failure with asset committed, or success) but the asset owner can always at any point commit the asset, thereby effectively destroying its value. While some of these alternatives may be more attractive from a theory perspective, the current setup seems to be most realistic.

weak beliefs, on the other hand, will end up in a subordinate role: they put little value on control and are less likely to disobey. That is indeed what the following proposition shows.

To study this formally, I will assume that there is an infinite pool of potential players of which half have high confidence  $\bar{\nu}$  and half have low confidence  $\underline{\nu} < \bar{\nu}$ . Assumptions 1b and 1a hold for both  $\underline{\nu}$  and  $\bar{\nu}$ . I now look for a selection of two players (from that pool of potential players) and an allocation of ownership that maximizes the joint utility of the two selected players.

**Proposition 2** *A selection of players maximizes joint utility for all values of  $B$  if and only if it consists of one player with high confidence  $\bar{\nu}$  and one player with low confidence  $\underline{\nu}$ . In equilibrium, the high-confidence player has authority over the low-confidence player.*

**Proof :** Since lemma 1 distinguished the players' confidence, its results also apply directly to this case. Proposition 1 then extends (with the appropriate modifications to the wages) by an analogous proof. It follows that the equilibrium will be  $Au-P_i$  with or without effort. Consider without loss of generality  $Au-P_1$ . The total utility and the feasibility condition are  $U_{Au-1} = B + \tilde{\alpha}_1\nu_1 + \tilde{\alpha}_2\frac{1}{2}$  and

$$w \in \left[ \max \left( B + \tilde{\alpha}_1q - \underline{u}_1, \tilde{\alpha}_2 \left( \frac{(1-p)}{p} (2\nu_2 - 1) - (1 - \nu_2) \right) + \underline{u}_2 \right), \min(B + \tilde{\alpha}_1\nu_1 - \underline{u}_1, B) \right]$$

The proposition then follows by observing that increasing  $\nu_1$  and decreasing  $\nu_2$  increase the joint utility and relax the feasibility condition. Since  $U_{Au-1}$  strictly increases in  $\nu_1$ ,  $P_1$  must always have high confidence in any optimal selection of players. Moreover,  $\tilde{p}$  in the proof of proposition 1 increases in  $\nu_2$ , so that at least for some values of  $B$  only  $\nu_2 = \underline{\nu}$  is optimal. This proves the proposition. ■

The intuition behind this proposition is exactly the one set forth above. Note that this is a positive (rather than normative) result: it predicts who will tend to be in control. It does not say that such allocation is optimal from the perspective of a social planner (who may have beliefs as to which players are most likely to be correct).

**Allocating assets by auction or trade** The main analysis simply determined the asset allocation that maximizes the joint utility of all players. A more elaborate model could endogenize this asset allocation process as a non-cooperative game. It turns out that most traditional allocation processes, such as the 'efficient' multi-person bargaining process of Gul (1989) or an ascending-price auction, would result in exactly this utility-maximizing outcome.

**Moral hazard** The main model also limited the importance of moral hazard to keep the analysis simple and focused on firms. Van den Steen (2005) – which considers this issue in a closely related setting but without putting it in a theory-of-the-firm context and without assets – gives some indications of what would happen when moral hazard becomes much more important. In particular, it suggests that at some point there is a structural change in the equilibrium outcome from an 'authority' to a 'no authority' equilibrium. In the 'no authority' equilibrium, there is no more efficiency wage and no more orders or obedience, while the residual income is more shared as in the case of a partnership or independent agent. This issue requires more study in the current context.

## 4 Discussion

### 4.1 The Firm as a Legal Person

In the model and formal analysis, I followed Knight (1921) or Coase (1937) by not distinguishing formally between the firm and its entrepreneur-owner. Nevertheless, the model in this paper is (im-

plicitly) built on a very clear definition of the firm that draws a definite line between the firm and its owner(s). In particular, I define the firm as a legal entity or legal person.<sup>22</sup>

Being a legal person means that a firm is a legal fiction that has all the standing and abilities of a physical person, i.e., the firm is an ‘as if’ person: it can own assets; it can write contracts; it has rights and obligations; etc. There are two important differences between a firm and a physical person. First, a firm is owned by shareholders. Nevertheless, it is distinct from these shareholders and indivisible. No shareholder directly owns any assets of the firm or can unilaterally decide to take out assets. The second key difference is that a firm cannot act on its own. Instead, its powers are exercised by a manager appointed by the shareholders. Even though the manager signs contracts for the firm, these contracts bind the firm rather than the manager.

The implications of being a legal person are explored in more detail in Van den Steen (2007b), which builds on the current paper. It is useful to report some of the results here since they are relevant for the reach and interpretation of the theory.

The most important insight from that analysis is how the ‘authority theory of the firm’ of this paper easily and naturally extends to a firm that is owned by a group of shareholders, rather than by an individual entrepreneur. In particular, the firm as a legal person then aggregates asset ownership and, by doing so, allows the firm’s manager to act as the ‘as if’ owner of all assets and as the ‘as if’ party to all contracts (while simultaneously allowing the firm’s owners to keep a reasonable check on the manager’s behavior). The firm as a legal person thus captures the benefits of dispersed ownership in terms of income (such as diversification and weakening of budget constraints) without losing the benefits of concentrated ownership in terms of authority. To study this situation formally, Van den Steen (2007b) considers a setting with different types of players, where player types correspond to different mental models. Players of one type nearly always agree with each other, but disagree with a small probability. Players of different types have independent beliefs and thus disagree half the time, as in the model of this paper. One player can determine another player’s type at some cost. Players, finally, are risk-averse (so that there are benefits from diversification). In the equilibrium of that paper, then, a firm is always owned by a group of players of one type. This firm hires other players as employees (without determining their type). The paper also shows explicitly that asset ownership by the firm can dominate direct asset ownership by individual shareholders. In particular, direct ownership by shareholders not only allows these shareholders to block the manager’s decisions when they disagree, but it also causes employees to obey the relevant shareholders rather than the manager. Such disobedience is detrimental for coordination. And even though the probability of any particular shareholder disagreeing is small, the overall probability quickly grows as there are many shareholders. Apart from extending the theory to a multi-owner context, the paper thus provides an economic reason for the legal status of the firm.

Another insight from this ‘personal’ theory of the firm is a new perspective on firm boundaries. In particular, once a firm is defined as a legal person or legal entity, firm integration is defined as one legal person versus two. The integrated entity has all rights and obligations, including all contracts and ownership, of these two entities. The manager of the integrated entity is thus the ‘as if’ party to all contracts and the ‘as if’ owner of all the assets. While it is possible – and useful – to enumerate a firm’s rights and obligations (including ownership), translating these to strict and absolute boundaries is not necessary in this framework, given that it is already well-defined what it means to be one versus two firms. Moreover, a contract is never unambiguously ‘part’ of either party, since no party has residual control over the contract. In this framework, what matters is what the firm can do, rather than where it ‘ends’.

Van den Steen (2007b) models the firm as a legal entity explicitly. It does so by introducing a

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<sup>22</sup>This is the legal definition of a firm. My point (in particular in Van den Steen (2007b)) is that this legal definition is actually also a good starting point for an economic analysis of the firm.

new type of (passive) player in the game – the firm – which is owned by other players who appoint a physical player to ‘manage’ the firm and exercise its rights. When, however, the model is limited – as in this paper – to a single entrepreneur-owner who does not sell his firm, the legal person of the firm is indistinguishable from the physical person of the owner. For transparency reasons, the current paper therefore does not make the distinction explicit (any more).

## 4.2 Knight’s Theory of Entrepreneurship

It is difficult to avoid a comparison of this theory of the firm with Knight’s (1926) theory of entrepreneurship since the two have important themes in common.

The starting point is the observation that differing priors is one way to interpret Knight’s ‘uncertainty’ (as opposed to ‘risk’).<sup>23</sup> According to Knight, “(t)he conception of an objectively measurable probability [...] is simply inapplicable [to ‘uncertainty’]. The confusion arises from the fact that we do estimate the value or validity or dependability of our opinions or estimates, and such an estimate has the same *form* as a probability judgement [...]” (p.231). In the formality of this paper, a player will indeed have an opinion that, say,  $X$  is the most likely state and  $\nu$  is then his estimate of the dependability of that opinion. Knight also suggests to designate risk and uncertainty by “the terms ‘objective’ and ‘subjective’ probability” (p.233). These statements are consistent with an interpretation of ‘uncertainty’ and ‘estimate’ in terms of prior beliefs: your prior is your personal subjective estimate of some (currently) unknowable probability.

According to Knight, then, people differ (with respect to uncertainty) in the confidence in their judgment, which he described above as the ‘estimate [of the] dependability of [one’s] estimates’ and which is captured here by a player’s confidence  $\nu$ . Knight then describes “the most fundamental change of all in the form of organization” as the “system under which the confident (...) ‘insure’ the doubtful and timid by guaranteeing to the latter a specified income in return for an assignment of the actual results” (p.269). While this statement is often interpreted as referring to risk-neutral people insuring the risk-averse, such interpretation actually does not seem consistent with Knight’s interpretation of confidence, which refers to the probability that one’s estimate is correct and is thus clearly something different than risk neutrality. Moreover, the terms ‘doubtful and timid’ also don’t describe risk-aversion very well. Once we exclude risk-aversion, then one interpretation of Knight’s theory of entrepreneurship is exactly the form of employment described in this paper: the principal tells the agent what to do and – in exchange – gives the agent a fixed wage, i.e., he *insures* the agent against the principal’s mistakes. Note that, following the extension in section 3, it are indeed the more confident players who become the boss.

## 4.3 The Role of Interpersonal Authority

Economists often consider prices and contracting, rather than authority-like arrangements, as the default method to get things done. As Weitzman (1974) pointed out, however, lay people are more likely to consider more centralized arrangements first. The analysis in this paper suggests one reason why so many cooperative relationships in society are governed by interpersonal authority: all you need is a sufficiently high wage and a non-trivial possibility to end the cooperation. This is often much simpler/cheaper than a contract with state-contingent actions via message games etc.<sup>24</sup> Of course,

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<sup>23</sup>While Knight himself does not provide any clear formal definition of the concepts, but describes them in extensive prose, people have tried to concisely capture his definition of risk as ‘randomness with knowable probabilities’ and of uncertainty as ‘randomness with unknowable probabilities.’

<sup>24</sup>Other papers have taken this simplicity as given and studied further implications. Simon (1951), for example, studies when such interpersonal authority dominates direct contracting on actions. Wernerfelt (1997) builds on this simplicity of authority to develop a theory of firms versus markets.

studying such contracts is useful from a theoretical perspective, to understand what can be achieved and how.

Note that this paper does *not* imply that interpersonal authority is limited to within-firm relationships. I only argued that centralized asset ownership and low-powered incentives strengthen interpersonal authority, not that they are necessary conditions. It is perfectly possible for a firm to have some degree of authority over other firms or over non-employees. This may also require leaving the obeying party some rents combined with a threat of termination, as in Klein and Leffler (1981), but this issue requires further study.

#### 4.4 The Role of the Differing Priors Assumption

Another important issue is the role of differing priors in the results. In other words, which results depend on the differing priors assumption and which results extend beyond?

It is straightforward to see that the effect of asset ownership on interpersonal authority is quite general. It seems to extend, for example, to a setting where the principal-agent conflict is based on effort or on private benefits, or where the ‘contract’ is a relational contract in a repeated-game setting. Most of the other mechanisms in the paper do, however, depend on the assumption of differing priors or open disagreement. Consider first the mechanisms that cause low-powered incentives. Since allocating residual income to the agent aligns his objectives with those of the principal in a common priors setting, high-powered incentives will not cause disobedience, on the contrary. Second, since the principal and agent will value (in expectation) the residual income identically under common priors, this is also no reason any more to shift residual income to the principal. Consider next the mechanisms that drive – in this paper – the co-location of residual income and residual control. For these, I argued already earlier that open disagreement is a key element since that is what causes a player to want control and also what causes the different valuation of residual income based on who controls the decisions. Furthermore, as will be discussed later, the results on firm boundaries derived in section 6 depend, among other things, on how the Coase Theorem is affected by differing priors.

While the differing priors assumption plays an important role in this paper, it may well be possible to combine the asset ownership result with other mechanisms to derive a consistent theory of the firm that does not rely on differing priors. However, since most known arguments for low-powered incentives, co-location of control and income, and firm boundaries rely on very diverse principles, I have as yet not found a simple coherent way to do this. Furthermore, an extension to the case with multiple shareholders seems much more complex. This is an important topic for future research.

#### 4.5 Sorting and Culture

An obvious question is whether the manager couldn’t hire people with similar beliefs and thus avoid the whole disobedience and authority issue? The answer is that – just as with persuasion – this is a cost/benefit tradeoff. Sorting on beliefs is definitely possible and was explored in Van den Steen (2004a), which links this to ‘corporate culture’ as shared beliefs and values (Schein 1985, Kotter and Heskett 1992). But it is often also very expensive. In particular, beliefs are multi-dimensional and some beliefs may be very difficult to extract in a job-interview context. Who would admit that they do not trust other people or think that the average subordinate is not very smart? Sorting ex-post through turnover is also very costly since it destroys organizational and firm-specific human capital. In both cases, the cost of sorting rises exponentially with the quality of the match that is required.

Interpersonal authority may be much more cost-effective especially for less important positions and positions where independent motivation and initiative are not too important. I thus informally conjecture that interpersonal authority will be used more for low-level and routine jobs, while sorting on beliefs – just like persuasion – will be more common for higher positions with discretion over

important decisions. This definitely fits with casual empiricism. Top consulting firms, for example, use considerable resources on hiring new professionals. This hiring process is carried out by the professionals themselves – including the senior partners – rather than by the HR department. An important part of the process is making sure that the candidate ‘fits’. The hiring of administrative staff by these same firms takes much less resources and puts much less stress on fit. Note, however, that casual empiricism in such firms suggests that not even the best sorting process will be able to eliminate all disagreement. So, despite the use of sorting, authority will remain a useful and often necessary tool to manage coordinated actions, even on the highest level of the firm.

Overall, while shared beliefs and persuasion are thus alternatives to interpersonal authority, they will be used only in as far as they are more economical than direct interpersonal authority. Moreover, the prediction of this paper is that a firm is more likely to be observed exactly when authority is a useful tool.

## 5 Endogenous Outside Options

The model in the previous sections – with exogenous outside options – is in fact a reduced form for a richer model with endogenous outside options that I will present now. Besides endogenizing the outside options, I will also allow more players and more assets.

(Apart from the fact that it takes care of some formal details for working with multiple projects, this section is not necessary to follow the analysis on firm boundaries in section 6 or the discussion in section 7.)

### 5.1 The Full Model

In order to endogenize the outside options, I will embed the model of section 2 in a larger multi-period game where players can rematch if they end the project prematurely (i.e., when the bargaining breaks down or when someone ends the contract). Apart from these outside options, only stage 1 will be affected in a substantial way. (The other stages change slightly in response to the larger number of players and assets.)

Formally, consider now an economy with  $I$  players and two sets of  $A$  assets each, where I assume  $I \rightarrow \infty$  and  $A < \infty$ . Denote the two sets of assets as  $\mathcal{A}_1$  and  $\mathcal{A}_2$ . A ‘project’ is still a revenue stream  $R_n$  – with  $n$  indexing the projects – that requires two players (denoted  $P_{1,n}$  and  $P_{2,n}$ ) and two assets (denoted  $a_{1,n}$  and  $a_{2,n}$ ) with now one asset from each type, i.e.,  $a_{k,n} \in \mathcal{A}_k$ . Any two players with two assets can execute a project. As in section 2, the two participants make decisions  $D_{1,n}$  and  $D_{2,n}$ , and the probability of success  $Q_n$  of project  $R_n$  depends on these decisions being correct. (The probability  $Q_n \equiv 0$  if there are less than 2 players or less than two (different) assets. More players or more assets for one project, on the other hand, do not increase the probability.) To simplify the analysis, I will consider only the case of assumption 1a with  $\theta = 1$ , i.e., without moral hazard. In all other respects, the structure of the payoffs and beliefs are the same as in section 2. Let me thus turn to the timing, represented in figure 3.

As mentioned before, the first stage – with the contracting – is the part of the game that is affected most by this modification. In particular, with more assets and more players, the first stage is not only about negotiating a contract, but also about matching players and assets. To specify this, I will define a ‘bargaining solution’ to consist of

- A set of  $N$  projects,  $\mathcal{R} = \{R_1, \dots, R_n, \dots, R_N\}$ , with  $N \leq A$ .
- For each project  $R_n$ , a set of players  $I_n \subset I$  who are involved in the project.

- For each involved player  $i \in I_n$  a contract  $(\alpha_{i,n}, v_{i,n}, F_{i,n})$  where  $F_{i,n}$  is an up-front transfer,  $\alpha_{i,n} \in [0, 1]$ , and where the budget is balanced:  $\sum_{i \in I_n} \alpha_{i,n} = 1$ ,  $\sum_{i \in I_n} v_{i,n} = B$ ,  $\sum_{i \in I_n} F_{i,n} = 0$ .
- For each project, the two assets  $(a_{1,n}, a_{2,n})$  that will be used. No asset can be used in more than one project. The owner of each assets must be in  $I_n$ .
- For each project, the two players  $(P_{1,n}, P_{2,n})$  who take the two actions/decisions  $(D_{1,n}, D_{2,n})$ . No player can take actions/decisions in more than one project. Both players must be in  $I_n$ .
- For definiteness, any  $j \in I_n$  must be either one of the  $P_{i,n}$  or own one of the  $a_{k,n}$  or have  $(\alpha_{j,n}, v_{j,n}, F_{j,n}) \neq (0, 0, 0)$ .

Instead of formulating an explicit bargaining protocol, I will use the (efficient) Shapley solution.<sup>25</sup> The outside options are defined below. As to the timing itself, the bargaining solution gets determined in stage 1a, immediately after which the payments  $F_{i,n}$  get made.

Stage 2 and 3 are identical to the one in section 2, except for a few minor changes that relate to the fact that there are now multiple projects and more than 2 players. In particular, in step 2b, any player will now be able to send a cheap talk message from  $\{X, Y\}$  to any player with whom he is involved in a project. In step 2c and 3b, each player can end the contract for any *particular* project. In other words, a player can end one contract in which he is involved, but continue in his other projects. If any involved player ends the contract in stage 3b, then the project fails. For any project in which a player ends the contract, the game moves immediately to stage 4b. The two decision makers of a project (and the decision makers only) get intrinsic motivation  $\gamma \geq 0$  from the project's success.<sup>26</sup>

Stage 4b captures the outside options. In particular, the game returns to 1a but now with payoffs discounted by  $\delta \in (0, 1)$ , effectively starting a new period. If the game ended prematurely, then the assets were preserved and the owner of the assets can use his assets in the next period. Since project execution commits the assets that were used in that particular project, the set of assets will decrease over time and the game effectively ends when all assets are committed.

I will now assume that  $\delta > \frac{B+q}{B+\nu}$ . This assumption says essentially that a player (who is a claimant) gets a better payoff from getting both decisions right next period than from getting only one decision right this period. This is the assumption that gives  $\underline{u}(\{a_1, a_2\}) \geq B + q$  in section 2. Without this, it is sometimes impossible for a manager to commit to firing a disobeying employee. The essence of the results would hold without the assumption, but it would be necessary to distinguish different cases, and the complexity of the analysis would increase substantially. I will also assume the equivalent of assumption 1a, which can be written  $\gamma \leq \frac{p\tilde{\epsilon}}{4}$  for  $\tilde{\epsilon} = \min((1 - \delta)(B + \nu), B)$ . As before, I will focus on Pareto-efficient, pure-strategy equilibria in order to get meaningful cheap-talk and simplify the analysis.

## 5.2 Analysis

The result and the intuition of lemma 1 extend fairly directly to this setting. In particular, lemma 1 holds now on the level of a project, subject to two changes. First, all contract variables are made project specific:  $\alpha_{i,n}$  and  $v_{i,n}$  replace  $\alpha_i$  and  $v_i$ , etc. Second, the outside options are also project-specific: they are the expected revenues of the players if only this particular project ends prematurely.

There is also an important extension to lemma 1 for the case that someone other than the two decision makers has authority. To that purpose, let ‘Authority by  $i$ ’ (for  $i \notin \{P_{1,n}, P_{2,n}\}$ ) denote the

<sup>25</sup>There are some well-known bargaining protocols that implement the Shapley solution, such as Gul (1989) or Hart and Mas-Colell (1996).

<sup>26</sup>The implicit idea is that  $\gamma$  captures career benefits of decision makers. Alternative specifications are obviously possible and lead typically to small modifications of the results.

1	2	3	4
Contracting	Orders and Decisions	Execution	Payoffs
a Players and assets get matched into projects $R_n$ and the contracts $(\alpha_{i,n}, \nu_{i,n}, F_{i,n})$ get determined (using the Shapley solution). b The $F_{i,n}$ are paid. c The beliefs $\mu_i$ get (privately) drawn.	a Each player can send a cheap-talk message from $\{X, Y\}$ to any player with whom he is involved in a project. b Each player who has to make a decision for a project publicly chooses his action from $\{X, Y\}$ . c With probability $p$ , each player can end any particular contract in which he is involved. The game (for that project) then moves to stage 4b.	a State is realized, assets are committed. b Each player can end any particular contract in which he is involved. The project then fails and the game moves to 4b.	a The contract $(\nu_{i,n}, \alpha_{i,n})$ gets executed. b The game returns to stage 1a with payoffs discounted by $\delta$ (and with only the assets that were not committed).

Figure 3: Time line of the model with endogenous outside options

following equilibrium outcome:  $i$  orders both  $P_{1,n}$  and  $P_{2,n}$  what to do; both  $P_{1,n}$  and  $P_{2,n}$  obey  $i$ 's orders;  $i$  ends the contract if either  $P_{1,n}$  or  $P_{2,n}$  were to disobey (thereby ending the project); and no participant quits in equilibrium. The following lemma then determines, by extension of lemma 1, the conditions for ‘Authority by  $i$ ’. Let  $\check{\alpha}_j = \alpha_j + \gamma$  and remember that only decision makers  $P_{1,n}$  and  $P_{2,n}$  have intrinsic motivation  $\gamma$ .

**Lemma 2** *Consider a project  $R_n$  with players  $j$  and  $k$  as decision makers. ‘Authority by  $i$ ’ (with  $i \neq j, k$ ) is an equilibrium if and only if all of the following conditions are satisfied:*

- $v_{j,n} + v_{k,n} \in [B + \alpha_{i,n}q - \underline{u}_{i,n}, \min(B + \alpha_{i,n}\nu_{i,n} - \underline{u}_{i,n}, B)]$
- $v_{j,n} \geq \check{\alpha}_{j,n} (\kappa(2\nu_{j,n} - 1) - (1 - \nu_{j,n})) + \underline{u}_{j,n}$  and  $v_{k,n} \geq \check{\alpha}_{k,n} (\kappa(2\nu_{k,n} - 1) - (1 - \nu_{k,n})) + \underline{u}_{k,n}$

where  $\kappa = (1 - p)/p$ . Moreover, it is the unique (Pareto-efficient and pure-strategy) equilibrium on the interior of the interval. The joint utility  $U_n = B + \alpha_{i,n}\nu + (1 + 2\gamma - \alpha_{i,n})\frac{1}{2}$ .

**Proof :** From the proof of lemma 1, ‘Authority by  $i$ ’ is an equilibrium iff the following conditions hold.

First, all players stay if  $j$  and  $k$  obey  $i$ . For  $i$ , this requires that  $B + \alpha_{i,n}\nu_{i,n} - v_{j,n} - v_{k,n} \geq \underline{u}_{i,n}$  or  $v_{j,n} + v_{k,n} \leq B + \alpha_{i,n}\nu_{i,n} - \underline{u}_{i,n}$ . For  $j$ , this requires that  $\check{\alpha}_{j,n}(1 - \nu_{j,n}) + v_{j,n} \geq \underline{u}_{j,n}$  or  $v_{j,n} \geq -\check{\alpha}_{j,n}(1 - \nu_{j,n}) + \underline{u}_{j,n}$  and analogously for  $k$ :  $v_{k,n} \geq -\check{\alpha}_{k,n}(1 - \nu_{k,n}) + \underline{u}_{k,n}$ .

Second, all players stay even when the project turns out to be a failure. For  $i$ , this requires that  $B - v_{j,n} - v_{k,n} \geq 0$  or  $v_{j,n} + v_{k,n} \leq B$ . The condition for  $j$  is that  $v_{j,n} \geq 0$ . The same holds for  $k$ .

Third,  $i$  quits if either  $j$  or  $k$  disobeys, which requires that  $B + \alpha_{i,n}q - v_{j,n} - v_{k,n} \leq \underline{u}_{i,n}$  or  $B + \alpha_{i,n}q - \underline{u}_{i,n} \leq v_{j,n} + v_{k,n}$ .

Finally, both  $j$  and  $k$  obey (given that the other obeys). For  $j$ , this requires that  $\check{\alpha}_{j,n}(1 - \nu_{j,n}) + v_{j,n} \geq p\underline{u}_{j,n} + (1 - p)(\check{\alpha}_{j,n}\nu_{j,n} + v_{j,n})$  or  $v_{j,n} \geq \check{\alpha}_{j,n}(\kappa(2\nu_{j,n} - 1) - (1 - \nu_{j,n})) + \underline{u}_{j,n}$  and analogously for  $k$ . Note that this implies  $v_{j,n} \geq -\check{\alpha}_{j,n}(1 - \nu_{j,n}) + \underline{u}_{j,n}$ . Moreover, the assumption on  $p$  implies that  $\kappa(2\nu_{j,n} - 1) - (1 - \nu_{j,n}) \geq 0$  and thus  $v_{j,n} \geq 0$ .

Putting things together, ‘Authority by  $i$ ’ is an equilibrium if and only if the following conditions are satisfied:

- $v_{j,n} + v_{k,n} \in [B + \alpha_{i,n}q - \underline{u}_{i,n}, \min(B + \alpha_{i,n}\nu_{i,n} - \underline{u}_{i,n}, B)]$
- $v_{j,n} \geq \check{\alpha}_{j,n}(\kappa(2\nu_{j,n} - 1) - (1 - \nu_{j,n})) + \underline{u}_{j,n}$  and  $v_{k,n} \geq \check{\alpha}_{k,n}(\kappa(2\nu_{k,n} - 1) - (1 - \nu_{k,n})) + \underline{u}_{k,n}$

Note also that – following the proof of lemma 1 – if these conditions are satisfied, then the unique (Pareto-efficient, pure-strategy) equilibrium is ‘Authority by  $i$ ’ (except potentially in the end-points). This proves the proposition. ■

I now show that an appropriate version of proposition 1 also holds for this setting. To state that result formally, let  $o_i$  denote the set of assets owned by player  $i$ ;  $O = \{o_i\}_{i=1}^{\infty}$  a complete ownership structure;  $\mathcal{O} = \{O : \cup_{i=1}^{\infty} o_i = \mathcal{A}_1 \cup \mathcal{A}_2; \forall i \neq j, o_i \cap o_j = \emptyset\}$  the set of feasible asset allocations; and

$\bar{\mathcal{O}} = \{O \in \mathcal{O} : \forall i, \#(o_i \cap \mathcal{A}_1) = \#(o_i \cap \mathcal{A}_2)\}$  the ownership allocations such that the assets are owned in matching pairs, i.e., each player either owns no assets or owns exactly the assets that are necessary and sufficient for a set of projects. Moreover, let  $n_i = \#o_i \cap \mathcal{A}_1$ .

The following proposition then says that allocating assets in matching pairs to players is the only ownership allocation that maximizes the joint expected utility  $U$  for all parameter values. Moreover, the only equilibrium that then maximizes  $U$  for all values of  $B$  is such that for each project all residual income gets allocated to the project's 'owner'; owners hire others under a fixed-wage contract; the owner tells these other players what to do; and these non-owners obey. In other words, owners hire non-owners as employees and these employees take their orders from the owner. To clarify the proposition, I state the results in words between brackets.

**Proposition 3** *An ownership allocation  $O$  maximizes  $U$  for all values of  $B$  iff  $O \in \bar{\mathcal{O}}$ . For any  $O \in \bar{\mathcal{O}}$ , the only equilibria that maximize  $U$  for all values of  $B$  are as follows:*

- *For any  $i$  with  $n_i \geq 1$ ,  $\exists \mathcal{R}_i \subset \mathcal{R}$  with  $\#\mathcal{R}_i = n_i$  and s.t.  $\forall R_n \in \mathcal{R}_i: i \in I_n$  and  $a_{k,n} \in o_i$ , and  $\forall j \in \bigcup_{\mathcal{R}_i} I_n \setminus \{i\}: o_j = \emptyset$ . (For any player who owns assets, there exists a subset of the projects such that this player owns exactly all the assets for these projects.)*
- *For some  $R_{\hat{n}} \in \mathcal{R}_i: i \in \{P_{1,\hat{n}}, P_{2,\hat{n}}\}$ . For all  $R_n \in \mathcal{R}_i \setminus \{R_{\hat{n}}\}: \#I_n = 3$ . (Such player will be a decision maker on one of his projects. All his other projects have 3 participants.)*
- *For all  $R_n \in \mathcal{R}_i, \forall j \in I_n \setminus \{i\}: \alpha_{i,n} = 1, \alpha_{j,n} = 0, v_{j,n} = \gamma(\kappa(2\nu - 1) - (1 - \nu)), F_{j,n} = v_{j,n}$ . (Such player will get the full residual income from all his projects and pay an efficiency wage to his employees to neutralize their temptation to disobey that comes from their intrinsic motivation.)*
- *For all  $R_n \in \mathcal{R}_i$ , the equilibrium for the subgame starting in period 2 is 'Authority by  $i$ '.*
- *When  $\gamma > 0$ , then  $n_i \leq 1$ . (When players have non-trivial intrinsic motivation, then all projects will be owned by different players.)*

**Proof :** See appendix. ■

The outside option of a player is now  $\delta \bar{U}_{Au}/2$  times the number of assets that he or she owns. It follows that the conditions of section 2 that  $\underline{u}(\emptyset) = 0$  and  $0 < \underline{u}(\{a_1\}) + \underline{u}(\{a_2\}) = \underline{u}(\{a_1, a_2\}) < B + (1 + \gamma)\nu + \frac{\gamma}{2}$  arise indeed naturally from the model.<sup>27</sup> Furthermore, the assumption that  $\delta(B + \nu) > B + q$  implies the earlier assumption that  $\underline{u}(\{a_1, a_2\}) > B + q$ . So the model literally endogenizes the outside options of the earlier model.

Note that in this outcome, a player can 'own' more than one project. If a player does own multiple projects, then employees handle all decisions on all these projects but one. It is still, however, the owner who tells each employee what to do. In the setting above, such multi-project ownership only happens when players have no intrinsic motivation and then generates exactly the same value as a solution where each project is owned by a different player. That will change in the next section, where such 'merger' really affects expected residual income.

## 6 Fundamental Disagreement, Break-up, and Firm Boundaries

One important purpose of a theory of the firm is to provide foundations for 'markets versus hierarchies' decisions. In this section, I use the theory of this paper to propose the risk of 'break-up' as a new theory for integration.

<sup>27</sup>Note that the stated condition on the outside option was actually  $\underline{u}(\{a_1, a_2\}) < B + \nu$ . The condition on  $\gamma$ , however, made it sufficient to ensure that  $\underline{u}(\{a_1, a_2\}) < B + (1 + \gamma)\nu + \frac{\gamma}{2}$ .

This theory of break-up is motivated by personal observations of a real acquisition decision. In this case, the focal firm wanted to fill out its product line, and found another firm with a complementary product line. The focal company was considering either an alliance or an outright acquisition. The main perceived risk of an alliance, relative to an acquisition, was the fear of future ‘strategic differences’. In particular, both firms would have to make considerable relation-specific investments (integrating the product lines) and there was a risk that future disagreements could prove unresolvable and cause a break-up of the alliance. This issue was instrumental in the firm’s decision to choose an acquisition, in order to have full control. Among other things, this obviously raises the question why such disagreements could not be resolved through bargaining and contracting.

The purpose of this section, then, is to formalize this argument and show why, indeed, perfect ex-post contracting cannot attain the same results as changing firm boundaries. In particular, I will first show that open disagreement may cause two (separate) firms to go their own way despite cooperation (modelled as coordination) being optimal from the perspective of any outsider. Integration can resolve this issue by giving – in equilibrium – one manager interpersonal authority over all employees, and thus by eliminating disagreement among those in control.<sup>28</sup> Second, proposition 4c will show that integration can be strictly optimal *even when there is perfect and frictionless ex-post bargaining over the decisions* (and even absent incontractible investments that may cause holdup). The intuition is that due to their diverging beliefs, the two managers cannot agree how to cooperate (i.e., what to coordinate on) and – from each firm’s perspective – taking the wrong action is more costly than the *joint* coordination losses. This is an application of the results of Van den Steen (2007a) to this context of break-up. In particular, that paper shows that Coase’s (1960) celebrated examples for the Coase Theorem – that ownership is irrelevant when there is perfect bargaining on actions – may fail when people openly disagree. Ownership matters here despite frictionless bargaining.

This result is in marked contrast to the property rights theory of the firm (Grossman and Hart 1986, Hart and Moore 1990, Hart 1995) – where integration only matters in the presence of incontractible investments – and to Hart and Holmstrom (2002) or Baker, Gibbons, and Murphy (2006) where ex-post incontractibility is really necessary.

I then further show that this risk of breakup gets leveraged into an important additional effect: the anticipation of such break-up may prevent relation-specific investments since the parties may fear that they will not reap the benefits of the investment. Proposition 4d shows that this may make integration strictly optimal *even when these relation-specific investments are ex-ante contractible* (and either with or without frictionless ex-post bargaining on the decisions). This is again in contrast to the existing literature, where hold-up only matters when it is caused by *non-contractible* ex-ante investments.

While break-up has similarities to hold-up, it also has significant differences. In both cases, a key issue is that some players fear not to get the full return on their investment. While hold-up redistributes value, break-up causes some value not to be realized at all. One implication of this difference is that break-up is itself costly, while hold-up is costly only through its effect on investments. Another implication of this difference is that hold-up can be solved by ex-ante contractibility of the investments, but that that solution often does not work for break-up. In both senses, break-up is actually a harder issue.

To analyze this theory of firm boundaries formally, consider the following variation on the model of section 5. Assume that there are two potential projects with respective revenue streams  $R_1$  and  $R_2$ , and that each project requires exactly one asset. Denote the asset required for project  $R_n$  as  $a_n$ ,

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<sup>28</sup>Analogous to the property rights theory, the only change will be a shift in asset ownership. All other ‘changes’, including the changes in contracts, are really changes in the equilibrium outcomes.

Note that the cost of integration in this model is that one of the projects is not owned by its optimal owner when considered in isolation (i.e., the player with the clearest view about how to do this project). The benefit of integration is that it eliminates fundamental disagreement by giving all control to one player and thus guarantees coordination.



To express all these ideas formally, let  $d_{i,n}$  be the indicator function that decision  $D_{i,n}$  is correct, and let the respective probabilities of success (conditional on execution) for the two projects be  $Q_1 = (1 - \beta) \frac{d_{1,1} + \rho d_{2,1}}{2} + \beta I_{\{D_{2,1}=D_{2,2}\}}$  and  $Q_2 = (1 - \beta) \frac{\rho d_{1,2} + d_{2,2}}{2} + \beta I_{\{D_{2,1}=D_{2,2}\}}$ . To keep the analysis tractable, I will consider the case without moral hazard, i.e.,  $\theta = 1$ , and with negligible intrinsic motivation, i.e., the limit where  $\gamma \downarrow 0$ . The earlier assumption that  $\delta > \frac{B+q}{B+\nu}$  becomes a bit more complex due to the coordination issue and the different confidence levels:  $(1 - \delta) < \frac{\rho(\underline{\nu} - \frac{1}{2}) - \frac{\beta}{(1-\beta)}}{\frac{B}{(1-\beta)} + \frac{\nu + \rho \underline{\nu}}{2}}$  (which obviously requires  $\frac{\beta}{(1-\beta)} < \rho(\underline{\nu} - \frac{1}{2})$ ). Otherwise, the model is identical to that of section 5.

I now first establish that absent cooperation issues ( $\beta = 0$ ) the assets are optimally owned by players of different types. In other words – absent cooperation issues – it is strictly optimal to have two separate firms. The reason why separate ownership is optimal is that, in terms of the earlier example, type-1 players are more confident about product design decisions and thus have a higher expected value from ‘owning’ the more design-dependent project, while type-2 players are more confident about channel design decisions and thus have a higher expected value from ‘owning’ the more channel-dependent project (where ‘owning’ a project is meant as having the project’s full residual income and control, through asset ownership and contracting). Think Apple versus Dell. Since the projects are unrelated, separate ownership is thus optimal.

**Proposition 4a** *When  $\beta = 0$ , an allocation of asset ownership maximizes  $U$  for all values of  $B$  if and only if it allocates  $a_1$  to a player of type 1 and  $a_2$  to a player of type 2.*

**Proof :** Since – with  $\beta = 0$  – there is no connection between the two projects, I can treat each project separately. The analysis is then essentially analogous to the proof of proposition 3.

One important difference is that for each project  $U_n \leq B + \frac{\bar{\nu} + \rho \underline{\nu}}{2}$ . This expected utility level (only) gets attained when for, say, project  $R_1$  the equilibrium is ‘Authority by  $i$ ’ with  $i$  a player of type 1.<sup>29</sup> A completely analogous argument to that of proposition 3 then implies that the (only) ownership structure that implements this equilibrium and thus reaches this expected utility for all values of  $B$  is one in which  $i$  owns asset  $a_1$ . Repeating this argument for  $R_2$  implies that an ownership structure maximizes  $U$  (for all values of  $B$ ) if and only if it allocates  $a_1$  to a player of type 1 and  $a_2$  to a player of type 2. ■

When there are cooperation issues ( $\beta > 0$ ), however, an integrated firm may be strictly optimal. In particular, the following proposition says that for intermediate values of  $\beta$  it is uniquely optimal to have only one owner. The intuition for this result is as follows. Consider the situation with two separate firms, and assume that the firms’ managers disagree on the right course of action for decision  $D_{2,n}$ . Being different firms implies that each has full residual income and control for its project. As a consequence, a manager incurs a considerable cost from trying to coordinate since it requires him to make a decision that he deems suboptimal. Disagreement thus causes a conflict between the desire to make an optimal decision and the desire to coordinate. When one firm owns both assets, its manager always agrees with himself so that that conflict vanishes. That is exactly what integration accomplishes.

**Proposition 4b** *When  $\frac{(1-\rho)(\bar{\nu}-\underline{\nu})}{2} < \frac{\beta}{(1-\beta)} < \rho(\underline{\nu} - \frac{1}{2})$ , an allocation maximizes  $U$  for all values of  $B$  if and only if it allocates both assets to one player.*

**Proof :** An argument similar to before implies that there are two candidates for the optimal allocation, with accompanying equilibrium:

<sup>29</sup>To see that  $B + \frac{\bar{\nu} + \rho \underline{\nu}}{2}$  cannot be attained by giving authority over decision  $D_{1,1}$  to a player of type 1 and authority over  $D_{2,1}$  to a player of type 2, note that the project’s expected returns according to the respective players are  $B + \frac{\bar{\nu} + \rho \frac{1}{2}}{2}$  and  $B + \frac{\frac{1}{2} + \rho \bar{\nu}}{2}$ . No allocation of residual income can make the expected utility larger than  $B + \frac{\bar{\nu} + \rho \underline{\nu}}{2}$ .

1. Asset  $a_n$  gets allocated to a type- $n$  player. The owner (of project  $R_n$ ), denoted  $P_{1,n}$ , makes a  $(w, \alpha, F) = (0, 0, 0)$  offer to a non-owner, and the ensuing equilibrium is ‘Authority by  $P_{1,n}$ ’.
2. Both assets get allocated to one player. The owner, denoted  $P_1$ , makes  $(w, \alpha, F) = (0, 0, 0)$  offers to three non-owners, and the ensuing equilibrium is ‘Authority by  $P_1$ ’ (where  $P_1$  quits the project if any of the three disobeys).

Consider now first the situation that both assets are allocated to one player. Since  $D_{2,1}$  and  $D_{2,2}$  have the same state variable, this player will always coordinate the decisions. It follows that the expected revenue is  $2B + (1 - \beta)(1 + \rho)\frac{\bar{v} + \underline{v}}{2} + 2\beta$ .

Consider next the case that a type- $k$  player owns  $a_k$ . As long as  $\beta < (1 - \beta)\rho(\underline{v} - \frac{1}{2})$ , neither owner is willing to choose an action he considers less likely to succeed in order to achieve coordination. It follows that the total expected payoff from split ownership equals  $2B + 2(1 - \beta)\frac{\bar{v} + \rho\underline{v}}{2} + \beta$ , where the  $\beta$  comes from the fact that the players will agree, and thus automatically coordinate, half the time.

Finally, the merged firm gives higher total utility if  $2B + (1 - \beta)(1 + \rho)\frac{\bar{v} + \underline{v}}{2} + 2\beta \geq 2B + 2(1 - \beta)\frac{\bar{v} + \rho\underline{v}}{2} + \beta$  or  $\frac{\beta}{(1 - \beta)} \geq (1 - \rho)\frac{\bar{v} - \underline{v}}{2}$  ■

Note that integration has two effects that together drive the result. First, in equilibrium, the integrated company will be the residual claimant on both projects. Since both projects are now evaluated by one and the same manager, there can be no disagreement on the optimal course of action. Second, in equilibrium, integration also concentrates the necessary control, i.e., the one manager has interpersonal authority over all employees in both projects and can thus implement the coordinated actions.

**Ex-post bargaining and unresolvable disagreement** The intuition also suggests that frictionless ex-post bargaining over the decisions (i.e., bargaining at the time the decisions are made, after the uncertainty is realized) will not necessarily solve this issue: each firm remains the residual claimant on its project and thus bears the consequences of making a (in its eyes) suboptimal decision. It follows that a firm will still be faced with a conflict between trying to make the right decision and trying to coordinate. In particular, the following proposition identifies conditions under which integration is still strictly optimal.

**Proposition 4c** *When the decisions  $D_{i,n}$  are perfectly contractible at the end of step 2a but  $\frac{(1 - \rho)(\bar{v} - \underline{v})}{2} < \frac{\beta}{(1 - \beta)} < \rho\frac{\underline{v} - \frac{1}{2}}{2}$ , an allocation maximizes  $U$  (for all values of  $B$ ) if and only if it allocates both assets to one player.*

**Proof :** Consider first the case that the assets are separately owned (with a  $k$ -type player owning  $a_k$ ). If the owners would try to coordinate by contracting ex-post, they would contract such that the project that is least sensitive to the second (channel) decision, which is project  $R_1$ , follows the belief of the other owner. In other words, player  $P_{2,1}$  implements what the owner of  $R_2$  believes is best for  $D_{2,1}$ . This will be optimal if and only if  $2\beta \geq (1 - \beta)\rho(\underline{v} - q)$  where the LHS is the gain from coordination and the RHS is the cost of coordination to the owner who cares least about this particular decision (and who will thus be the one taking his less preferred action). So when  $\frac{\beta}{(1 - \beta)} < \rho\frac{\underline{v} - \frac{1}{2}}{2}$  then the separate firms will not coordinate when their managers disagree.

The condition for the integrated firm to generate higher  $U$  remains the same as in proposition 4b:  $\frac{\beta}{(1 - \beta)} \geq (1 - \rho)\frac{\bar{v} - \underline{v}}{2}$ . This concludes the proposition. ■

This is thus an ‘unresolvable disagreement’: even if decisions are contractible, the players will not come to an agreement and will lose the benefits from cooperation. The driving force here is that each firm remains the residual claimant on its own project and thus bears the full costs of following a suboptimal (from its manager’s point of view) course of action. When this (subjective) cost is larger than the benefits from cooperation, then they will not cooperate. In the integrated firm, on the other hand, cooperation always happens, as before. The issue here is thus not a failure of bargaining, as with private information, but a change in what is subjectively optimal. This is an application of Van

den Steen (2007a), which shows how Coase's own examples for the Coase Theorem (Coase 1960) may fail under open disagreement and which, based on this paper's model, shows how firm integration may solve trade failures caused by disagreement.

**Relation-specific Investments** This break-up issue becomes even more significant when there are relation-specific investments. In particular, the anticipation of break-up may prevent such investments and thus strengthen the case for integration.

To see this formally, assume that getting the benefits from cooperation require an up-front investment  $b$  by, say, the firm that owns asset  $a_1$ . (The cooperation benefit, however, still only obtains if the firms actually coordinate). The following proposition then says that a merged firm is more likely to make the relation-specific investment, that integration can be strictly optimal, and that that still holds *even when* I allow perfect ex-ante contractibility of the investments and frictionless ex-post bargaining on the decisions.

**Proposition 4d** *The set of parameters for which the separate firms invest is a strict subset of the set of parameters for which the merged firm invests, whether or not the investment is ex-ante contractible and whether or not the decisions are contractible at the end of step 2a.*

Assume that  $\frac{(1-\rho)(\bar{v}-\underline{v})}{2} < \frac{2\beta-b}{(1-\beta)}$ ,  $\frac{\beta}{(1-\beta)} < \rho \frac{\underline{v}-\frac{1}{2}}{2}$ ,  $\beta < b < 2\beta$ , the investment is perfectly contractible (prior to stage 1), and the decisions are contractible at the end of step 2a. In that case, an allocation maximizes  $U$  for all values of  $b$  if and only if it allocates both assets to one player.

**Proof :** Consider first a merged firm. It will always coordinate and it will invest if  $b \leq 2\beta$ . Consider next two separate firms. From the earlier propositions, it follows that they will coordinate absent ex-post bargaining (on the decision) if  $\frac{\beta}{(1-\beta)} \geq \rho(\underline{v} - \frac{1}{2})$  and with ex-post bargaining if  $\frac{\beta}{(1-\beta)} \geq \rho \frac{\underline{v}-\frac{1}{2}}{2}$ . Moreover, if they do not (always) coordinate and the investment is not contractible, then the firm that owns  $a_1$  invests if  $b \leq \frac{\beta}{2}$ . If they either (always) coordinate and the investment is non-contractible or they do not (always) coordinate but the investment is contractible, then they invest if  $b \leq \beta$ . Finally, if they do (always) coordinate and the investment is contractible then they invest whenever the merged firm invests. It follows that whenever the separate firms invest, so will the merged firm. But there is a part of the parameter space (with non-empty interior) where the merged firm invests but the separate firms do not. This proves the first part of the proposition.

For the second part of the proposition, consider the case that the firms can contract on the investment and can contract ex-post on the decision. By the earlier calculations, separate firms will not coordinate even if they can contract ex-post whenever  $\frac{\beta}{(1-\beta)} < \rho \frac{\underline{v}-\frac{1}{2}}{2}$ . Second, conditional on separate firms not coordinating upon disagreement, the above implied that a merged firm will invest but separate firms will not invest, even if the investment is contractible, whenever  $\beta < b < 2\beta$ . Finally, some algebra implies that the expected value from a merged firm that makes the investment is larger than the expected value of separate firms that do not make the investment when  $\frac{(1-\rho)(\bar{v}-\underline{v})}{2} < \frac{2\beta-b}{(1-\beta)}$ . This proves the proposition. ■

The reason why ex-ante contractibility of the investment cannot solve the problem is that the risk of break-up still remains. As long as the parties cannot commit to align their decisions in the future, the up-front investments are not worth making. Of course, the issue will be more important and apply more broadly when investments and ex-post decisions are *not* contractible.

Overall, the potential for future unresolvable disagreement and break-up can prevent relation-specific investments, even if the investments are perfectly contractible and even if there is frictionless ex-post bargaining over the decisions. The prediction that the need for relation-specific investments leads to integration has found support in, for example, Monteverde and Teece (1982).

## 7 Relationship to Other Theories of Firm Boundaries

One final issue is how this theory interacts with other theories of the firm and of firm boundaries. While it is impossible to treat this issue here in full, even a short discussion of some of the most prominent theories is probably useful. In what follows, I will mainly focus on the theories highlighted by Gibbons (2005). The key point of the discussion is to show that this theory is highly complementary to theories based on rent-seeking, adaptation, or incentives, while it is compatible – in a more orthogonal sense – with the property rights theory.

Consider first the property rights theory of Grossman and Hart (1986), Hart and Moore (1990), and Hart (1995). For the case of an entrepreneur-owner, the theory in this paper integrates quite easily – though without much interaction – with the property rights theory. In particular, if – in the model of this paper – the player can make investments prior to the *contracting* stage, then asset ownership will give investment incentives very similar to these in the GHM property rights model. Things get more complex when considering a larger firm with multiple shareholders, however. In particular – as pointed out by Holmstrom (1999) and Hart and Holmstrom (2002) – the property rights theory is essentially about individuals – rather than firms – owning assets. This is an issue for further research.

Consider next the rent-seeking and hold-up models in the style of Klein, Crawford, and Alchian (1978) or Williamson (1985). Combining the multi-project setup of section 6 (with  $\beta = 0$ ) with a ‘costly rent-seeking’ model in the style of Masten (1986) suggests that such rent-seeking models integrate well with the current theory. More importantly, it seems that the two theories enrich each other. In one direction, the current theory may provide formal answers to Hart’s (1995) criticism of the rent-seeking models. In particular, it suggests a formal answer how firm boundaries affect authority and rent-seeking and it can simultaneously endogenize the cost of integration in the form of a suboptimal allocation of individual projects (from a standalone perspective). In the other direction, the rent-seeking models provide complementary predictions on firm boundaries for this ‘authority theory of the firm’.

A somewhat similar relationship exists with the adaptation theory (Simon 1951, Williamson 1975). Consider a multi-project setup similar to section 6 (again with  $\beta = 0$ ) where a decision of one project has implications for the other project, but the exact magnitude of the implication will become clear only later in the game. Prior to the game, the parties can write a contract on that decision, but contractibility vanishes once the game starts (due, for example, to time pressure). The decision on firm boundaries will now depend on the need for adaptation. Also in this case, the current paper suggests formal micro-foundations for the adaptation story, while the adaptation theory provides complementary predictions. The same is true for theories, such as Hart and Holmstrom (2002), that assume that ownership of physical assets somehow conveys control over the projects that use these assets. While the Hart-Holmstrom assumption is uncontroversial for single-person projects, it is more problematic for large projects that require the non-trivial participation of a group of people. In that case, control over the project requires interpersonal authority over people. The current paper provides micro-foundations for why ownership of assets would indeed convey interpersonal authority over people, and thus allows to apply these theories to larger projects.

The relationship to the incentive theory of firm boundaries (Holmstrom and Milgrom 1994, Holmstrom 1999) is in some sense even tighter. In particular, imagine that some decisions affect, among other things, the value of an asset. Asset ownership by an employee is then similar to high-powered incentives and will thus lead to disobedience. This shows that the essential idea of the asset-incentives theory translate nearly literally to the current context.

Overall, apart from delivering a self-contained theory of the firm that is fully consistent with a differing prior interpretation of Knight’s view, the theory in this paper is thus also a strong complement to some of the major perspectives on firm boundaries outlined in Gibbons (2005).

## 8 Conclusion

This paper presented a theory of the firm in which unified asset ownership by a firm and low-powered incentive contracts for its employees serve the purpose of giving the firm's manager interpersonal authority over its employees. In doing so, the theory also provides micro-foundations for the idea that bringing a project in a firm gives the manager interpersonal authority over the employees working on the project. It complements a number of theories on firm boundaries which rely on that assumption, such as theories of rent-seeking and rent-seeking-style hold-up (Klein, Crawford, and Alchian 1978, Williamson 1985) or theories of adaptation (Simon 1951, Williamson 1975). I also argued that Knight's view of entrepreneurship can be interpreted along the lines of this theory of the firm.

This theory of the firm also allowed me to propose a new economic theory for firm boundaries: the risk of break-up. In particular, even when cooperation is always optimal from any outsider's perspective, open disagreement may prevent such cooperation between independent firms. Integration solves this by eliminating disagreement at the top. A key result is that this failure to cooperate may persist – and integration thus be strictly optimal – *even when the actions are perfectly ex-post contractible*. In other words, perfect contractibility of actions cannot substitute for a change in firm boundaries. This application of Van den Steen (2007a) makes economic sense of the notion – often expressed by managers – that managers may prefer outright mergers and acquisitions because they feel they need full control over the other firm if they will depend on it. The anticipation of such break-up may furthermore prevent relation-specific investments – even contractible ones – and thus further strengthen the case for integration.

The underlying definition in this paper of the firm as a legal person is further developed in Van den Steen (2007b). That paper shows how this definition of the firm as a legal entity allows extending the current theory to a setting with multiple shareholders. It shows, in particular, how and why the firm's owning the assets can dominate each individual shareholder's directly owning part of the assets. In other words, it shows how the firm *aggregates* ownership and contracts to let the manager act 'as if' he is the (sole) owner of all assets and party to all contracts. The paper also treats some related issues, such as the definition of firm boundaries in this context and the possibility of firms without any assets.

The current paper also raised some further research questions. Section 4 suggested, apart from the definition of a firm as a legal entity, the issue of authority between firms. Contrasting authority between firms with authority within firms should improve our understanding of firm boundaries, especially in relation to other arrangements such as alliances. This also raises the issue of other ownership structures such as partnerships or consumer cooperatives. Section 6 raises the obvious issue of firm boundaries. Klepper and Thompson (2006) provide interesting evidence on the role of strategic disagreement in the formation of new firms through spinoffs.<sup>30</sup> I believe that the current theory raises some interesting conjectures in that direction.

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<sup>30</sup> Although not stressed in the paper, their model assumes differing priors with regard to the precision of the information.

## A Proofs

**Proof of Lemma 1:** For later purposes, I will distinguish in this proof the confidence of both players,  $\nu_1$  and  $\nu_2$ , and the intrinsic motivation of both players,  $\gamma_1$  and  $\gamma_2$ .

Consider first stage 4a. A player  $P_i$  will exert effort if the project is a success,  $(\alpha_i + \gamma_i)(1 - \theta) \geq e$ , and he believes that the other player will also exert effort. Since we consider only equilibria that are not Pareto-dominated, both players will exert effort (upon success) iff  $\min_i(\alpha_i + \gamma_i)(1 - \theta) \geq e$ . Let now  $\eta = 1$  and  $\tilde{e} = e$  if  $\min_i(\alpha_i + \gamma_i)(1 - \theta) \geq e$  and  $\eta = \theta$  and  $\tilde{e} = 0$  otherwise. Let finally  $\tilde{\alpha}_i = (\alpha_i + \gamma_i)\eta - \tilde{e}$ , so that  $\tilde{\alpha}_i$  is  $P_i$ 's expected payoff from a success net of his/her potential cost of effort.

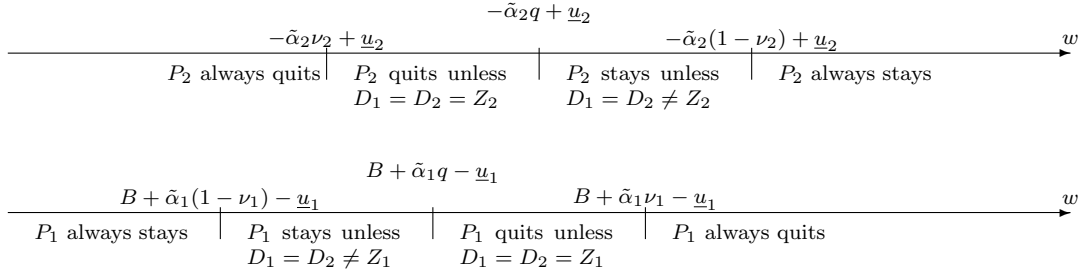
Consider next stage 3b.  $P_1$  quits upon failure if  $B - w < 0$  or  $w > B$ , and upon success if  $B + \tilde{\alpha}_1 - w < 0$  or  $w > B + \tilde{\alpha}_1$ , while  $P_2$  quits upon failure if  $w < 0$  and upon success if  $w + \tilde{\alpha}_2 < 0$  or  $w < -\tilde{\alpha}_2$ . Note that if  $w \notin [0, B]$ , then  $w$  gets only paid upon success. In what follows, I do the analysis assuming that  $w \in [0, B]$  and then consider at the end the case that  $w \notin [0, B]$ .

Consider now stage 2c. If  $i$  believes that  $D_i = D_j = Z_i$ , then  $u_i = \tilde{\alpha}_i\nu_i + v_i$  and  $P_i$  stays if  $\tilde{\alpha}_i\nu_i + v_i \geq \underline{u}_i$ . If  $D_i \neq D_j$  then  $u_i = \tilde{\alpha}_iq + v_i$  and  $P_i$  stays if  $\tilde{\alpha}_iq + v_i \geq \underline{u}_i$ . If  $D_i = D_j \neq Z_i$ , then  $u_i = \tilde{\alpha}_i(1 - \nu_i) + v_i$  and  $P_i$  stays if  $\tilde{\alpha}_i(1 - \nu_i) + v_i \geq \underline{u}_i$ .

Consider now, for example, player  $P_1$ . If  $D_1 = D_2 = Z_1$ , then he stays if  $B + \tilde{\alpha}_1\nu_1 - \underline{u}_1 \geq w$ . If  $D_1 \neq D_2$  then he stays if  $B + \tilde{\alpha}_1q - \underline{u}_1 \geq w$ . If  $D_1 = D_2 \neq Z_1$ , then he stays if  $B + \tilde{\alpha}_1(1 - \nu_1) - \underline{u}_1 \geq w$ . In other words,

- if  $w \leq B + \tilde{\alpha}_1(1 - \nu_1) - \underline{u}_1$  then he always stays
- if  $B + \tilde{\alpha}_1(1 - \nu_1) - \underline{u}_1 \leq w \leq B + \tilde{\alpha}_1q - \underline{u}_1$  then he stays unless the worst happens ( $D_1 = D_2 \neq Z_1$ )
- if  $B + \tilde{\alpha}_1q - \underline{u}_1 \leq w \leq B + \tilde{\alpha}_1\nu_1 - \underline{u}_1$  then he stays only if the best happens ( $D_1 = D_2 = Z_1$ )
- if  $B + \tilde{\alpha}_1\nu_1 - \underline{u}_1 \leq w$  then he never stays

The conditions for  $P_2$  are analogous. This can be summarized graphically as follows, where the upper and lower graph may line up differently depending on  $\underline{u}_1$  and  $\underline{u}_2$ .



In an abuse of notation, I will use  $-$  in what follows  $- [a, b]$  to mean  $[a, b]$  when  $b \geq a$  and  $\emptyset$  otherwise.

If  $w \notin Z = [-\tilde{\alpha}_2\nu_2 + \underline{u}_2, B + \tilde{\alpha}_1\nu_1 - \underline{u}_1]$ , then at least one player quits for sure and the payoff is simply  $\underline{u}_1 + \underline{u}_2$ . So let's consider now  $w \in Z$ .

Let  $X = [-\tilde{\alpha}_2q + \underline{u}_2, B + \tilde{\alpha}_1q - \underline{u}_1]$ . Note that  $X \subset Z$ . If  $w \in X \subset Z$ , then neither player quits when the other disobeys (as long as he himself did what he thinks was best), so it is optimal for each player  $P_i$  to choose  $Z_i$ . Note that since orders have no impact, players prefer not to give orders. So the unique equilibrium is for no player to give orders, each player  $P_i$  to do  $Z_i$ , and neither player to quit. This is thus a 'No Authority-Stay' ( $NAu - Stay$ ) equilibrium.

Consider now the case that  $w \in [B + \tilde{\alpha}_1q - \underline{u}_1, B + \tilde{\alpha}_1\nu_1 - \underline{u}_1]$ , so  $P_1$  quits unless  $D_1 = D_2 = Z_1$ . It follows that  $-$  in any equilibrium where  $P_1$  does not quit for sure  $- P_1$  will always choose  $D_1 = Z_1$ . So there's two possible type of equilibria: those where  $P_2$  obeys and those where  $P_2$  does as he likes (and  $P_1$  quits if they disagree). Consider first the possibility of a 'Authority by  $P_1$ ' ( $Au - 1$ ) equilibrium. This requires that  $P_2$  always stays and prefers to obey. Always staying requires  $w \geq -\tilde{\alpha}_2(1 - \nu_2) + \underline{u}_2$ . Preferring to obey requires  $\tilde{\alpha}_2(1 - \nu_2) + w \geq p\underline{u}_2 + (1 - p)(\tilde{\alpha}_2\nu_2 + w)$  or  $w \geq \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2$  which implies  $w \geq -\tilde{\alpha}_2(1 - \nu_2) + \underline{u}_2$ . So  $P_1 - Au$  is an equilibrium (and the unique one on the interior) when  $w \in [\max(B + \tilde{\alpha}_1q - \underline{u}_1, \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2), B + \tilde{\alpha}_1\nu_1 - \underline{u}_1]$ .

Consider next the possibility of a ‘No Authority-Quit’ ( $NAu - Quit$ ) equilibrium, where  $P_2$  chooses  $Z_2$  but  $P_1$  quits when they take different actions. This ‘No Authority-Quit’ equilibrium requires – beyond the conditions already specified – that  $P_2$  stays upon agreement and prefers not to obey. Staying upon agreement requires  $w \geq -\tilde{\alpha}_2\nu_2 + \underline{u}_2$  so that overall, we need  $w \in [\max(-\tilde{\alpha}_2\nu_2 + \underline{u}_2, B + \tilde{\alpha}_1q - \underline{u}_1), \min(B + \tilde{\alpha}_1\nu_1 - \underline{u}_1, \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2)]$ . Analogous results obtain for  $P_1$ .

So if  $w \in [0, B]$  then we have (only) the following equilibria (where it is not ex-ante known that players will quit) and equilibrium conditions:

1.  $Au - 1$  if  $w \in [\max(B + \tilde{\alpha}_1q - \underline{u}_1, \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2), B + \tilde{\alpha}_1\nu_1 - \underline{u}_1]$ . The total expected payoff is then  $U_{Au-1} = B + \tilde{\alpha}_1\nu_1 + \tilde{\alpha}_2\frac{1}{2}$
2.  $Au - 2$  if  $w \in [-\tilde{\alpha}_2\nu_2 + \underline{u}_2, \min(-\tilde{\alpha}_2q + \underline{u}_2, B - \tilde{\alpha}_1(\kappa(2\nu_1 - 1) - (1 - \nu_1)) - \underline{u}_1)]$ . The total payoff is then  $U_{Au-2} = B + \tilde{\alpha}_2\nu_2 + \tilde{\alpha}_1\frac{1}{2}$
3.  $NAu - Stay$  if  $w \in [-\tilde{\alpha}_2q + \underline{u}_2, B + \tilde{\alpha}_1q - \underline{u}_1]$ . The total payoff is then  $U_{NAu-Stay} = B + \frac{\tilde{\alpha}_1\nu_1 + \tilde{\alpha}_2\nu_2 + (\tilde{\alpha}_1 + \tilde{\alpha}_2)q}{2}$
4.  $NAu - Quit$  if  $w \in [\max(-\tilde{\alpha}_2\nu_2 + \underline{u}_2, B + \tilde{\alpha}_1q - \underline{u}_1), \min(B + \tilde{\alpha}_1\nu_1 - \underline{u}_1, \tilde{\alpha}_2(\kappa(2\nu_2 - 1) - (1 - \nu_2)) + \underline{u}_2)]$  or if  $w \in [\max(-\tilde{\alpha}_2\nu_2 + \underline{u}_2, B - \tilde{\alpha}_1(\kappa(2\nu_1 - 1) - (1 - \nu_1)) - \underline{u}_1), \min(-\tilde{\alpha}_2q + \underline{u}_2, B + \tilde{\alpha}_1\nu_1 - \underline{u}_1)]$ . The total payoff is then  $U_{NAu-Quit} = \frac{B + \tilde{\alpha}_1\nu_1 + \tilde{\alpha}_2\nu_2}{2} + p\frac{\underline{u}_1 + \underline{u}_2}{2} + (1 - p)\frac{B + (\tilde{\alpha}_1 + \tilde{\alpha}_2)q}{2}$

If  $w \notin [0, B]$ , then  $w$  is paid only upon success so that it becomes a share of the residual income. Moreover, at least one player will quit upon failure in stage 3b, so that  $B$  is lost in that case. It follows that  $w \notin [0, B]$  is Pareto-dominated by a contract where  $w$  is included in  $\alpha$  so that  $\tilde{\alpha}_i = \alpha_i + \gamma_i + v_i$  and  $w = 0$ .

These conditions are indeed the ones of the lemma (taking into account that  $\kappa(2\nu_2 - 1) - (1 - \nu_2) > 0$  so that the lower bound 0 for  $Au - 1$  and the upper bound  $B$  for  $Au - 2$  are dominated).

Let  $\hat{U}_e$  and  $\hat{U}_{ne}$  denote the maximal joint (expected) utility of an authority equilibrium with and without effort and let  $\hat{U}_{NAu}$  denote the maximal joint utility of the respective no-authority equilibrium. For later purposes, I will now show that in the absence of  $w$ -constraints (including being able to freely choose the type of players in the case of proposition 2),  $\hat{U}_{ne} > \max(\hat{U}_{NAu-Stay}, \hat{U}_{NAu-Quit})$  and (in the case with moral hazard, i.e., assumption 1b)  $\hat{U}_e > \hat{U}_{ne}$ . Note that if  $\hat{U}_{ne} > \max(\hat{U}_{NAu-Stay}, \hat{U}_{NAu-Quit})$  under assumption 1b then it will also hold under 1a, so it suffices to consider only assumption 1b.

I will now first argue that, if there are different player-types with different levels of confidence as in proposition 2, it suffices to consider only the player-type with the highest confidence  $\bar{v}$ . Consider first  $\hat{U}_{ne}$  and  $\hat{U}_e$  for, say,  $Au - 1$ . Note that neither depends on  $\nu_2$  and both are increasing in  $\nu_1$ . It follows immediately that  $\hat{U}_{ne} = B + (1 + \gamma)\theta\bar{v} + \gamma\theta\frac{1}{2}$ .

For  $\hat{U}_e$  with  $Au - 1$ , we would get  $\hat{U}_e = B + (\alpha_1 + \gamma - e)\bar{v} + (\alpha_2 + \gamma - e)\frac{1}{2}$ . Effort requires that  $\min_i(\alpha_i + \gamma) \geq \frac{e}{(1 - \theta)}$ . Since moving residual income from  $P_2$  to  $P_1$  increases  $\hat{U}_e$  we get that  $\alpha_2 = \frac{e}{(1 - \theta)} - \gamma$  and thus  $\alpha_1 = 1 - \frac{e}{(1 - \theta)} + \gamma$  in any such equilibrium with effort. For this to be feasible (in particular, to make sure that  $P_1$  also exerts effort) requires that  $\alpha_1 \geq \frac{e}{(1 - \theta)} - \gamma$  or  $1 + 2\gamma \geq 2\frac{e}{(1 - \theta)}$  which is implied by assumption 1b. It then follows that  $\hat{U}_e = B + (1 - \frac{e}{(1 - \theta)} + 2\gamma - e)\bar{v} + (\frac{e}{(1 - \theta)} - e)\frac{1}{2} = B + (1 + 2\gamma - \frac{(2 - \theta)e}{(1 - \theta)})\bar{v} + \frac{\theta e}{(1 - \theta)}\frac{1}{2}$ .

Consider next  $NAu$ . Absent any constraints, both  $NAu - Stay$  and  $NAu - Quit$  are maximized when both players have the maximal confidence  $\bar{v}$ . The allocation of residual income then affects  $\hat{U}_{NAu}$  only through its impact on effort. Given this, the fact that effort is efficient, and the fact that  $\frac{e}{(1 - \theta)} \leq \frac{1}{2}$ , there will always be effort in equilibrium. The utilities are then  $U_{NAu-Stay} = B + (1 + \gamma_1 + \gamma_2 - 2e)\frac{\bar{v} + q}{2}$  and  $U_{NAu-Quit} = \frac{B + (1 + \gamma_1 + \gamma_2 - 2e)\bar{v}}{2} + p\frac{\underline{u}}{2} + (1 - p)\frac{B + (1 + \gamma_1 + \gamma_2 - 2e)q}{2}$ .

For  $NAu - Quit$ , it follows that

$$\begin{aligned} \hat{U}_{ne} - \hat{U}_{NAu-Quit} &= B + (1 + \gamma)\theta\bar{v} + \gamma\theta\frac{1}{2} - \frac{B + (1 + 2\gamma - 2e)\bar{v}}{2} - p\frac{\underline{u}}{2} - (1 - p)\frac{B + (1 + 2\gamma - 2e)q}{2} \\ &= \frac{B + \bar{v} - \underline{u}}{2} - (1 - \theta)\bar{v} + \frac{\gamma\theta}{2} + (e - (1 - \theta)\gamma)\bar{v} + (1 - p)\frac{(\underline{u} - B - q) - 2\gamma q + 2eq}{2} \\ &\geq \frac{\epsilon}{2} - (1 - \theta)\bar{v} + \frac{\gamma\theta}{2} + (e - (1 - \theta)\gamma)\bar{v} + (1 - p)\frac{\epsilon - 2\gamma q}{2} \end{aligned}$$

Assumption 1b implies that  $(1 - \theta) \leq \frac{\epsilon}{2}$ ,  $\gamma \leq \frac{\epsilon}{(1-\theta)}$ , and  $\epsilon \geq 2\gamma q$  so that indeed  $\hat{U}_{ne} > \hat{U}_{NAu-Quit}$ . For  $NAu$ -Stay, it follows that

$$\begin{aligned}\hat{U}_{ne} - \hat{U}_{NAu-Stay} &= B + (1 + \gamma)\theta\bar{v} + \gamma\theta\frac{1}{2} - B - (1 + 2\gamma - 2e)\frac{q + \bar{v}}{2} \\ &= \theta\bar{v} - \bar{v} + \frac{\bar{v} - q}{2} + \left(\gamma\theta\frac{1}{2} + \gamma\theta\bar{v} - 2\gamma\frac{q + \bar{v}}{2}\right) + e(q + \bar{v}) \\ &\geq \frac{2\epsilon}{2} - (1 - \theta)\bar{v} - 2\gamma\end{aligned}$$

where I use that (by assumption 1b)  $\bar{v} - q = B + \bar{v} - \underline{u} + \underline{u} - B - q \geq 2\epsilon$ . Assumption 1b implies that  $(1 - \theta) \leq \frac{\epsilon}{2}$  and  $\gamma \leq \frac{\epsilon}{4}$  so that indeed  $\hat{U}_{ne} > \hat{U}_{NAu-Stay}$ .

Consider finally  $Au$ - $P_1$  under assumption 1b. (The analysis and result for  $Au$ - $P_2$  is completely analogous.) The difference in utility is now

$$\begin{aligned}\hat{U}_e - \hat{U}_{ne} &= B + (1 + 2\gamma - \frac{(2 - \theta)e}{(1 - \theta)})\bar{v} + \left(\frac{\theta e}{(1 - \theta)}\right)\frac{1}{2} - B - (1 + \gamma)\theta\bar{v} - \gamma\theta\frac{1}{2} \\ &= \left((1 - \theta)(1 + \gamma) + \gamma - \frac{(2 - \theta)e}{(1 - \theta)}\right)\bar{v} + \theta\left(\frac{e}{(1 - \theta)} - \gamma\right)\frac{1}{2}\end{aligned}$$

Assumption 1b implies that  $(1 - \theta) \geq \frac{\epsilon}{(1-\theta)} + e$  and  $\gamma < \frac{\epsilon}{(1-\theta)}$  so that indeed  $\hat{U}_e > \hat{U}_{ne}$ . This finalizes the proposition.  $\blacksquare$

**Proof of Proposition 3:** The proof will follow the same pattern as the proof of proposition 1. I will first show that the allocation of ownership and equilibrium proposed in the proposition do indeed maximize  $U$ . I will then show that for some values of  $B$ , it is the only allocation and equilibrium to do so.

Let  $U_n$  denote the joint expected utility that all players in  $I_n$  derive from  $R_n$ . Considering all possible equilibria implies  $U_n \leq \bar{U}_{Au} = B + (1 + \gamma)\nu_1 + \frac{\gamma}{2}$ . Note, second, that any asset can be used only once for productive purposes. Third, delaying the execution of a project reduces the value generated due to discounting and the fact that the matching possibilities (may) go down. It follows that the maximum feasible value for  $U$  is  $U \leq A\bar{U}_{Au}$ . Note that the proposed equilibrium does indeed generate  $U = A\bar{U}_{Au}$ , so it is a matter of showing that this is indeed an equilibrium when  $O \in \bar{O}$ . Consider first the outside options. Since this game starts with an equal number of assets of each type, and assets get committed in pairs, there will always be an equal number of assets of each type. With  $I \rightarrow \infty$ , the assets are the resources in short supply. In the limit as  $I \rightarrow \infty$ , the Shapley value depends then only on asset ownership, allocates all value to asset owners, and does so in proportion to the number of assets owned. It follows that for each pair of assets, i.e. in each particular project, a participant's outside option equals  $\delta\bar{U}_{Au}$  if he owns the matching assets and 0 if he does not. (If the equilibrium generates  $U_n = \bar{U}_{Au}$  for  $R_n$ , then the increase in outside value from owning one extra asset is  $\delta\frac{\bar{U}_{Au}}{2}$ .)

Since the projects are completely unrelated, it suffices to focus now on a single project. Consider first the case that  $i$  is not a decision-maker, and let the two decision-makers be  $j$  and  $k$ . The conditions for 'Authority by  $i$ ' are now, given that in the proposed equilibrium  $\alpha_{j,n} = \alpha_{k,n} = \underline{u}_{j,n} = \underline{u}_{k,n} = 0$  and  $v_{j,n} = v_{k,n} = \gamma(\kappa(2\nu - 1) - (1 - \nu))$

- $v_{j,n} + v_{k,n} \in [B + (1 + \gamma)q - \underline{u}_{i,n}, \min(B + (1 + \gamma)\nu_{i,n} - \underline{u}_{i,n}, B)]$
- $v_{j,n} \geq \gamma(\kappa(2\nu - 1) - (1 - \nu))$  and  $v_{k,n} \geq \gamma(\kappa(2\nu - 1) - (1 - \nu))$

The last two conditions are trivially satisfied, while the first requires

$$2\gamma(\kappa(2\nu - 1) - (1 - \nu)) \in [B + (1 + \gamma)q - \underline{u}_{i,n}, \min(B + (1 + \gamma)\nu_{i,n} - \underline{u}_{i,n}, B)]$$

Since the assumption that  $\delta(B + \nu) > B + q$  implies that  $\delta(B + (1 + \gamma)\nu) > B + (1 + \gamma)q$  and thus  $B + (1 + \gamma)q - \underline{u}_{i,n} < 0$ , it suffices to show that

$$2\frac{\gamma}{p} \leq \min(B + (1 + \gamma)\nu_{i,n} - \delta(B + (1 + \gamma)\nu + \frac{\gamma}{2}), B)$$

where I used the observation that  $\kappa(2\nu - 1) - (1 - \nu) \leq \frac{1}{p}$ . It thus suffices that

$$2\frac{\gamma}{p} + \frac{\delta\gamma}{2} \leq \min((1 - \delta)(B + (1 + \gamma)\nu), B)$$

which is implied by  $\frac{\delta\gamma}{2} \leq \frac{2\gamma}{p}$  and by the assumption that  $\gamma \leq \frac{p\tilde{\epsilon}}{4}$  for  $\tilde{\epsilon} = \min((1 - \delta)(B + \nu), B)$ .

Consider next the case that  $i$  is himself a decision-maker on the project. Let the other decision maker be  $j$ . Note that this implies that  $\underline{u}_{j,n} = 0$  while  $\underline{u}_{i,n} = \delta\bar{U}_{Au}$ . The condition for ‘Authority by  $i$ ’ is then, given that in the proposed equilibrium  $\alpha_{j,n} = 0$ ,  $v_{j,n} = \gamma(\kappa(2\nu - 1) - (1 - \nu))$ ,

$$v_{j,n} \in [\max(B + (1 + \gamma)q - \underline{u}_{i,n}, \gamma(\kappa(2\nu_{j,n} - 1) - (1 - \nu_{j,n}))), \min(B + (1 + \gamma)\nu_{i,n} - \underline{u}_{i,n}, B)]$$

which is satisfied by the earlier argument (since this is a weaker constraint).

I’m now left to show that this is the only allocation and the only equilibrium that maximize  $U$  for all values of  $B$ . To see this, note first that the above implies that  $U = A\bar{U}_{Au}$  is always achievable. Furthermore, since the Shapley solution chooses a Pareto-efficient point in the feasible set, it will – in any subgame perfect equilibrium of an allocation that maximizes  $U$  – select a contract that implements  $U_n = \bar{U}_{Au}$  for all projects. This implies, first of all, that (for  $I \rightarrow \infty$ ) the outside options are  $\delta\frac{\bar{U}_{Au}}{2}$  per asset that a player owns. It implies, second, that in any equilibrium, all projects must be executed in the first period and the subgame equilibrium for each project must be an ‘Authority’-type equilibrium where the player with authority, say  $i$ , gets the full residual income, i.e.  $\alpha_i = 1$ . Note that once the bargaining solution is determined, each project is completely independent of the others. So I will focus on one project  $R_n$  and will argue that when  $B < \frac{\delta(B + \nu)}{2}$ , the solution proposed in the proposition is indeed the only one that implements ‘Authority by  $i$ ’. Any player – other than  $i$  – who owns an asset requires at least  $v_{k,n} \geq \frac{\delta\bar{U}_{Au}}{2} \geq \frac{\delta(B + \nu)}{2}$  which is impossible to satisfy given the requirements that (in any  $Au - i$  equilibrium)  $\sum_{j \in I_n \setminus \{i\}} v_{j,n} \leq B$  and  $v_{j,n} \geq 0$ . But that means that  $i$  must own the pair of matching assets that is used in  $R_n$ . Moreover, when  $\gamma > 0$ , then the situation where the asset owner is also a decision maker gives a higher utility ( $U = B + (1 + \gamma)\nu + \frac{\gamma}{2}$ ) than the situation where the asset owner is not a decision maker ( $U = B + \nu + \gamma$ ). Aggregating these conditions over all projects imply the proposition. ■

## B The Role of Authority in Asset Ownership and Incentives

Section 3 raised the possibility that the asset concentration and low-powered incentives may be caused completely by the optimal allocation of residual income rather than by the need for interpersonal authority. The way to distinguish the two effects is by comparing the original model to a benchmark model in which obedience is simply contractible. Any difference between the two must be caused by (the potential for) disobedience and thus by the need to generate authority. The following proposition makes exactly that comparison. In particular, it compares the original game to one with one modification: as part of the contract in step 1a, the players can contract that one player will obey the orders of the other (which implicitly assumes that both orders and actions are verifiable). Obviously, this is not meant as a realistic model but only as an analytical device. The proposition then shows that the need for authority indeed increases the need for low-powered incentives and for concentrated asset ownership. To state the result formally, let  $\hat{\alpha}$  denote the equilibrium choice of  $\alpha$  at the optimal asset allocation and  $\hat{O}$  the set of optimal ownership structures.

**Proposition 5** • *The set of parameters for which  $\hat{\alpha} = 0$  is strictly larger when obedience is not contractible.*

• *The set of parameters for which  $O_{ij} \notin \hat{O}$  with  $i \neq j$  is strictly larger when obedience is not contractible.*

**Proof :** Since obedience being contractible does not affect the conditions under which players will quit in stage 2c or 3b, lemma 1 implies that the type of equilibria and the joint utility that an equilibrium generates remain unchanged. The conditions under which a specific equilibrium is feasible, however, may change. Most importantly, the condition for  $Au - P_1$  now becomes  $w \in [\max(-\tilde{\alpha}_2(1 - \nu_2) + \underline{u}_2, 0), \min(B + \tilde{\alpha}_1\nu_1 - \underline{u}_1, B)]$ . (Note that  $w \geq -\tilde{\alpha}_2(1 - \nu_2) + \underline{u}_2$  is the condition that makes  $P_2$  stay when he disagrees with an order, while the obedience and the firing condition have dropped out.)

The fact that the types and joint utility of equilibria doesn't change implies that  $\hat{U}_{ne} > \max(\hat{U}_{NAu-Stay}, \hat{U}_{NAu-Quit})$  and (in the case with moral hazard, i.e., assumption 1b)  $\hat{U}_e > \hat{U}_{ne}$  absent  $w$ -constraints extend to this case. In what follows, I will use  $Au-P_i-e$  to denote 'Au- $P_i$  with both players exerting effort',  $Au-P_i-ne$  to denote 'Au- $P_i$  with no player exerting effort',  $OnC$  to denote the case that 'obedience is not contractible' and  $OC$  to denote the case that 'obedience is contractible'.

In view of proposition 1 and the symmetry of the game, it suffices for the first part of the proposition to show that 1)  $Au-P_1-ne$  is always feasible, and 2) the set of parameters for which  $Au-P_1-e$  is feasible is strictly larger under  $OC$  than under  $OnC$ .

To show now that  $Au-P_1-ne$  is always feasible, consider  $O = O_{11}$  and  $\alpha = 0$ . The feasibility condition is then  $w \in [\max(-\gamma\theta(1-\nu_2), 0), \min(B+(1+\gamma)\theta\nu_1-\underline{u}, B)]$ . Since the assumption on  $\theta$  implies that  $B+(1+\gamma)\theta\nu_1 > \underline{u}$ , this condition is always satisfied by  $w = 0$ .

To see that  $Au-P_i-e$  is feasible for a larger set of parameters under  $OC$ , I will actually show that it is always feasible under  $OC$ . To see this, note that when  $O = O_{11}$ ,  $\tilde{\alpha}_2 = e/(1-\theta)$ , and thus both players exerting effort, the feasibility condition is

$$w \in \left[ \max\left(-\left(\frac{e}{1-\theta} - e\right)(1-\nu_2), 0\right), \min\left(B + (1+2\gamma - \frac{e}{1-\theta} - e)\nu_1 - \underline{u}, B\right) \right]$$

For this to hold, it suffices that  $B + \nu_1 - \underline{u} + 2\gamma\nu_1 - \frac{(2-\theta)e}{1-\theta}\nu_1 \geq 0$  or  $\epsilon \geq \frac{(2-\theta)e}{1-\theta}$ , which follows from the assumptions. This indeed implies that, at the optimum asset allocation, the equilibrium is always an  $Au-P_i-e$  equilibrium. It follows that  $\hat{\alpha} > 0$  for all parameters when obedience is contractible. The first part of the proposition then follows from the fact that, following proposition 1,  $\hat{\alpha} = 0$  for a non-empty set when obedience is non-contractible.

Consider now the ownership structure. Note that  $O_{ij}$  with  $i \neq j$  can be only be optimal when it gives the same equilibrium as  $O_{ii}$  (since I showed above that the maximal utility can always be achieved with  $O_{ii}$ ). Consider first a set of parameters where the optimal equilibrium for both  $OC$  and  $OnC$  is  $Au-P_i-e$ . If under  $OnC$  the equilibrium remains  $Au-P_i-e$  when going to  $O_{ij}$ , then that must necessarily also hold for  $OC$  since the feasibility constraint is weaker in that latter case. So the result holds for any such set of parameters. Consider next a set of parameters where the equilibrium for  $OC$  is  $Au-P_i-e$ , while the equilibrium for  $OnC$  is  $Au-P_i-ne$ . (Since the equilibrium under  $OC$  is always  $Au-P_i-e$ , these are the only two possibilities.) I now have to show that if the  $OnC$  equilibrium does not change when moving to an  $O_{ij}$  ownership structure (so that  $O_{ij}$  is also optimal under  $OnC$ ), then that also holds for the  $OC$  equilibrium (so that, as above, the set where  $O_{ij}$  is optimal is larger under  $OC$ ). I will actually show more in general that whenever  $Au-P_i-ne$  is feasible under  $O_{ij}$  and  $OnC$ , then  $Au-P_i-e$  is feasible under  $O_{ij}$  and  $OC$ . Note that the first implies that the following interval is non-empty:

$$w \in \left[ \max\left(B + (1+\gamma)\theta q - \frac{\underline{u}}{2}, \gamma\theta(\kappa(2\nu_2-1) - (1-\nu_2)) + \frac{\underline{u}}{2}, 0\right), \min\left(B + (1+\gamma)\theta\nu_1 - \frac{\underline{u}}{2}, B\right) \right]$$

while the second requires that the following interval is non-empty

$$w \in \left[ \max\left(-\left(\frac{e}{1-\theta} - e\right)(1-\nu_2) + \frac{\underline{u}}{2}, 0\right), \min\left(B + (1+2\gamma - \frac{e}{1-\theta} - e)\nu_1 - \frac{\underline{u}}{2}, B\right) \right]$$

The result then follows from the fact that  $\gamma\theta(\kappa(2\nu_2-1) - (1-\nu_2)) + \frac{\underline{u}}{2} > -\left(\frac{e}{1-\theta} - e\right)(1-\nu_2) + \frac{\underline{u}}{2}$  and  $B + (1+\gamma)\theta\nu_1 - \frac{\underline{u}}{2} < B + (1+2\gamma - \frac{e}{1-\theta} - e)\nu_1 - \frac{\underline{u}}{2}$  where the latter follows from the fact that  $(1+\gamma)(1-\theta) + \gamma > \frac{2-\theta}{1-\theta}e$  which follows from the assumption that  $e \leq \frac{(1-\theta)^2}{2}$ .

For a case where  $O_{ij}$  is optimal under  $OC$  but not under  $OnC$ , consider  $B = \frac{\underline{u}}{2} < \theta\nu$ . Proposition 1 showed that, for  $OnC$ ,  $Au-1$  is then impossible under  $O_{ij}$ . So it suffices to show that  $Au-1$  is feasible under  $O_{ij}$  for  $OC$ . This requires that  $w \in \left[ \max\left(-\frac{\theta e}{1-\theta}(1-\nu_2) + \frac{\underline{u}}{2}, 0\right), \min\left(B + (1+2\gamma - \frac{(2-\theta)e}{1-\theta})\nu_1 - \frac{\underline{u}}{2}, B\right) \right]$  which is indeed feasible under these conditions. This completes the proof. ■

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